Providing Location-Privacy in Opportunistic Mobile Social Networks

by

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Abstract

Users face location-privacy risks when accessing Location-Based Services (LBSs) in an Opportunistic Mobile Social Networks (OMSNs). In order to protect the original requester’s identity and location, we propose two location privacy obfuscation protocols utilizing social ties between users.

The first one is called Multi-Hop Location-Privacy Protection (MHLPP) protocol. To increase chances of completing obfuscation operations, users detect and make contacts with one-hop or multi-hop neighbor friends in social networks. Encrypted obfuscation queries avoid users learning important information especially the original requester’s identity and location except for trusted users. Simulation results show that our protocol can give a higher query success ratio compared to its existing counterpart.

The second protocol is called Appointment Card Protocol (ACP). To facilitate the obfuscation operations of queries, we introduce the concept called Appointment Card (AC). The original requesters can send their queries to the LBS directly using the information in the AC, ensuring that the original requester is not detected by the LBS. Also, a path for reply message is kept when the query is sent, to help reduce time for replying queries. Simulation results show that our protocol preserves location privacy and has a higher query success ratio than its counterparts.

We have also developed a new OMSN simulator, called OMSN Routing Simulator (ORS), for simulating OMSN protocols more efficiently and effectively for reliable performance.
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Chapter 1

Introduction

Location-privacy is becoming a major concern in the Opportunistic Mobile Social Network (OMSN, which is a kind of a Delay Tolerant Network (DTN) [6] featuring lack of continuous connectivity. More specifically, in OMSNs, it is not necessary for senders to have an end-to-end routing path to their destinations. Users make contact when they encounter each other. LBSs are common applications in OMSNs and they are widely used in “military and government industries, emergency services and the commercial sector” [24], especially after the proliferation of localization technologies, like GPS. Many people access LBSs with their portable devices and send their location to LBS providers. In this case, LBS users face a continuous risk that their location may be leaked from the LBS applications, which makes people unwilling to use LBSs. Thus, protecting location privacy has been a critical issue in LBSs.

1.1 Motivation and Objective

LBSs which use the location information of users can be considered as “two types of application design: push and pull services” [24]. For example, you may receive an advertisement when you enter an area, which is a push service; if you look for the nearest restaurant, you
must pull information from the network. It is obvious that you must reveal your location if you use LBS. When you use a LBS application to find the nearest restaurant, you actually tell the LBS provider your location and your next destination which might have a restaurant nearby. If attackers can access the LBS provider’s database, they can learn that information. Then you may receive a lot of advertisements from surrounding restaurants.

Such inference attack, in addition to bothering you with advertisements, can become more dangerous when you send more queries to the LBS provider. If you use an LBS application several times in a day, the attackers can learn your trace from the information so that they can infer more information including your identity and home address. According to [12], “Hoh used a database of week-long GPS traces from 239 drivers in the Detroit, MI area. Examining a subset of 65 drivers, their home-finding algorithm was able to find plausible home locations of about 85%, although the authors did not know the actual locations of the drivers’ homes”. Therefore, the LBS provider is considered as a semi-trusted party so that users must protect their location-privacy when they use LBS applications.

The OMSN is defined “as decentralized opportunistic communication networks formed among human carried mobile devices that take advantage of mobility and social networks to create new opportunities for exchanging information and mobile ad hoc social networking” [22]. In other words, OMSN is a kind of mobile ad hoc network, and the information and technology of social network are also used in it. People carrying smartphones which contain WiFi or Bluetooth can form a typical OMSN. Since the WiFi, Bluetooth on smartphones can be used for discovering other devices and direct communication between devices, users can communicate with others who are within their communication range without using any infrastructure, which is the basic requirement of an OMSN. Since users in OMSN could also use LBS applications, their location-privacy must be protected. Besides, the information in the social network allows users to identify friends. Therefore, it is necessary to have location-privacy protection protocol using the social networks.
1.2 Objectives

Disconnection, decentralization and highly delays are obvious features for OMSN so that a decentralized strategy may benefit for the location-privacy protection protocol in OMSN. Besides, decreasing interactions between users and servers can significantly cut down the time cost. To prevent the attackers from learning users’ private information, the protocol should obfuscate users’ location and hide their identities.

1.3 Contributions

We propose two new decentralized location-privacy protecting protocols for OMSN so that they do not need a three-party server which is used to obfuscate queries for users. We also create a new simulator for OMSNs called OMSN Routing protocols Simulator (ORS) to evaluate our protocols.

The first protocol we propose is a distributed location-privacy algorithm called Multi-Hop Location-Privacy Protection (MHLPP), which achieves a higher query success ratio and guarantees location-privacy. The introduction of social networks enables us to hide the original requester’s information behind his friends. When a user wants to send a query, he starts to look for friends based on information in his social network. He sends his query to the first encountered friend who is then responsible for forwarding the query to the intended location. This friend can also pass the query to one of his friends when they encounter. When the distance between the user carrying this query and the original requester exceeds a specified threshold, the user sends the query to the LBS server directly without having to find a friend to pass on. At that time, he also replaces the original requester’s information with its own identity and location, which enables the LBS server to receive the query without any information about the original requester. After receiving the query, the LBS server replies to the last friend (the user sending the query to the LBS)
who then transmits it to the original requester.

Our second protocol is also a distributed location-privacy algorithm called Appointment Card Protocol (ACP), which aims to guarantee location-privacy and reach a higher query success ratio. The introduction of social networks enables us to hide the original requester’s information behind his friends. We introduce the Appointment Card (AC) as a kind of intermediary which records a series of agents. The original requester sends his query using the identity of the first agent in the AC to the LBS, which prevents the LBS from learning the identity of the requester. The reply of the query can be delivered back to the original requester through the same series of agents as in the AC. The last agent, called the trusted agent, is a user of the original requester, in the social network; in other words, he is a friend (or a friend of friends) of the original requester. The trusted agent separates the stranger-agents from the original requester so that no stranger knows the identity of the original requester. The query-delivery success ratio of our ACP is as good as that of any no-privacy protocol used in comparison in our experiment.

Our new simulator ORS is inspired by a well-known simulator, ONE [11], which is used by many researchers to test their models and protocols in DTN. The major reason why we created a new simulator is that the ONE is not designed for OMSN and lacks social networking concepts for it to be effective in OMSN. Adding social network information into the ONE simulator must modify its basic structure, which is problematic and might not ensure correctness of our experiments. We used more efficient algorithms to make our simulator run two times faster than ONE.

1.4 Thesis Organization

This thesis is organized as follows:

Chapter 2 describes the concept of Mobile Ad hoc networks, Delay Tolerant Networks,
Location-Based Services and social networks. We also give an overview of the existing location-privacy protocols.

Chapter 3 describes our first protocol, MHLPP, in detail. The performance of MHLPP has been compared against its counterpart, Hybrid and Social-aware Location-Privacy in Opportunistic mobile social networks (HSLPO) [31].

Chapter 4 elaborates on the second protocol, ACP. We describe how it works and how it enhances the location-privacy. Its performance is compared against Binary Spray and Wait (BSW) [25], distributed social based location privacy protocol (SLPD) [30], and our Multi-Hop Location-Privacy Protection (MHLPP).

Chapter 5 describes our new simulator which has been instrumental in simulating MHLPP and ACP in realistic settings. We introduce the key enhancements and the algorithms which are used in the simulator for making it more efficient.
Chapter 2

Background and Related Work

2.1 Mobile Ad hoc Networks

“Ad hoc networks are infrastructure-less and cooperation-based networks which means that the network topologies must be decided by the network sensors themselves” [33]. In other words, the major feature of ad hoc networks is that they have no infrastructures.

The Mobile Ad hoc NETwork (MANET), also called the Wireless Ad hoc NETwork (WANET), is a decentralized wireless network with no pre-existing infrastructure. In MANET, because users move independently, the topology changes frequently. Without the help of infrastructure, users can only communicate when they encounter each other. In other words, users communicate only if they are covered by each other’s communication range. Because of the above characteristics, the MANET can be viewed as a kind of Delay-Tolerant Network (DTN) that lacks continuous network connectivity. The MANET can hardly establish instantaneous end-to-end paths, which compels the routing protocols in MANET to use a “store-and-forward” strategy in which users forward messages when they encounter others, or they store messages for later delivery. As shown in Figure 2.1, the user $A$ has a message for $C$ but does not know where $C$ is, so he sends the message to $B$ when they encounter each other. The user $B$ then stores the message and moves along.
The message is then delivered to $C$ when both $B$ and $C$ come in contact with each other at a later time. It is obvious that whether the message can be delivered depends on the movement of the users. If $B$ will never meet $C$ or the message is held by a user for a long period of time, it must be dropped after some timeout. The delivery process can lead to low success ratio and is often time-consuming.

![Figure 2.1: MANET](image)

2.2 Delay Tolerant Network

Regular networks, e.g. Internet, always have end-to-end paths. As shown in Figure 2.2(a), two nodes $S$ and $D$ are connected through nodes $A$, $B$, and $C$. The maximum round-trip time is not excessive, and their drop probability is also small. Compared to the regular network, there is a class of challenged networks [6] which lack end-to-end path and suffer from high latency and long queuing delays. As shown in Figure 2.2(b), when node $B$ is down or non-existent, there is no connection between nodes $A$ and $C$, for which extensive latency is inevitable if the source $S$ sends a message to the destination $D$. 
Since the challenged networks are significantly different from the regular networks, researchers have introduced a new architecture, called Delay Tolerant Network (DTN), to deal with the unique features of the challenged networks. Terrestrial Mobile Networks, Exotic Media Networks, Military Ad Hoc Networks and Sensor/Actuator Networks are examples of typical DTNs.

2.2.1 Spray and Wait Protocol

The Spray and Wait [25] is a well-known protocol for message dissemination in DTNs. Although it is not as efficient as protocols on Internet, it works quite well in DTNs. A message is initialized with several copies, a part of which are given to others when users encounter each other. Users keep forwarding copies until they each have only one copy of the message. When a user carrying at least one copy of the message encounters the destination, he gives all his copies to the destination to complete the delivery. The Binary Spray and Wait (BSW) [25] is an optimized version of the Spray and Wait, which we use for comparison in this thesis. The user who creates the message also makes several copies of that message. He gives half of his copies to the user whom he encounters so that both he and the other user have half of the copies. The users who get copies of the message continue to give half of their copies to others until someone has only one copy to pass on to the destination.
2.2.2 Other DTN Protocols

2.2.2.1 Direct Contact Scheme

The simplest strategy for DTN is that the source holds the message until he meets the destination, which is called the direct contact scheme. So, a direct path between the source and the destination is necessary for a successful delivery. It is possible that the source never comes in contact with the destination in which case the message is not delivered.

2.2.2.2 Replica Based Protocols

The replica based protocols (e.g., [9], [13], [27], [15], and [20]) work by making several replicas of the message so that users can retransmit them upon connection establishment. The former BSW is also a kind of replica based protocols. Compared to the direct contact scheme, the replica-based protocols make it easy for messages to be delivered. But, they require more resources than the direct contact scheme because they need more memory to store the replicas. Therefore, making a reasonable decision on the message replication is the key to success of these kinds of protocols.

2.2.2.3 Knowledge-Based Protocols

Different from the former replica protocols which require no knowledge about the topology of the network, the users in knowledge-based protocols try to evaluate their own view of the topology of the network so that they can make better forwarding decisions, e.g. [29], [10] and [16]. However, the topology changes so frequently that it is hard for users to have an accurate topology.
2.2.2.4 Coding Based Protocols

Authors in [14] and [2] have suggested the approach that introduces coding techniques into the routing protocols. Instead of making a few replicas, coding based protocols encrypt data to make a large number of message blocks. If the destination receives a part of the blocks, he can decrypt the message.

2.3 Location-Based Services

The Location-Based Services (LBS) use users’ location information to provide services as shown in Figure 2.3. Your smartphone can detect your coordinate and send it to LBS application server which is responsible for providing service based on the coordinate. The point of interest and the location advertisement are familiar instances of LBS. The LBS providers collect users’ location information to provide service, which makes LBS providers a significant target of attack. When attackers access the databases of the LBS providers, they can learn all sensitive information in the servers. So, the LBS providers should be viewed as semi-trusted, which might expose information in front of vicious attackers.

Users face risks of information breach when they access a semi-trusted LBS provider because anyone who has access to data in LBSs is able to steal and misuse LBS users’ location-privacy. Considering that LBSs rely on location-aware computing, it is unavoidable to leak users’ location from LBSs. Therefore, balancing “these two competing aims of location privacy and location awareness” [4] is always a challenge.
2.4 Social Networks

Social networks which contain social interactions and personal relationships are used in location-privacy protection so that users can determine who can or cannot be trusted. In [28], the relationship of a pair of people (e.g., user $i$ and user $j$) is described as a pair of directed relationship strength. The directed relationship strength from the user $i$ to the user $j$ can be denoted by $RS^{ij}$. We should notice that $RS^{ij}$ might not be equal to $RS^{ji}$, because the user $i$ might like the user $j$ very much while the user $j$ just views the user $i$ as an acquaintance. Based on the relationship strength, it is possible to estimate the relational tie between two people and predict whether they are friends or strangers.

The relationship strength is compared with a threshold; if the relationship strength is higher than the threshold then the two people are friends, otherwise they are strangers. In the protocols we mention in the thesis, researchers always assume that friends are trustful. That is reasonable because you might feel more secure when your friends forward your message instead of a stranger.
2.5 Location-Privacy Protocols

The basic idea of most location-privacy protocols is hiding the original requester behind a set of users so that attackers can hardly infer the identity of the original requester. In other words, when a user sends a query, his identity cannot be inferred based on the information in the query easily. For example, the original requester can use a pseudonym instead of his real name or use an obfuscated location to send his queries, so that attackers cannot tell the difference between two sets of queries.

The location-privacy protocols are considered centralized and distributed based on whether they require any infrastructure for operation.

2.5.1 Centralized Protocols

Centralized protocols always need some infrastructure for the obfuscation process. The infrastructure could be any equipment which acts as an anonymization server. When the user wants to send a query to the LBS server, he sends the query to the anonymization server. The anonymization server changes the identity and the location in the query, which is called anonymization or obfuscation. Then, the anonymization server forwards the modified query to the LBS server, so that the attacker who attacks the LBS server can hardly learn the identity of the original requester. The LBS server can send the reply message to the anonymization server which is responsible for forwarding the reply message back to the original requester. In this way, the original requester gets the information he needs, while avoiding from being located by the attackers.

The advantage of a centralized protocol is that the anonymization server has more resources and information than users in the network, which enable the server to achieve better anonymization performance and provide sufficient protection for users. For example, if the anonymization server knows locations of all users in the network, it can modify the
location and identity in the queries to the most suitable, with which the LBS server can provide acceptable results while the original requester is not exposed.

There are two major shortcomings of these kinds of protocols: i) it is hard to deploy infrastructure in some areas, ii) since the anonymization server knows users’ location, it is also a risk for the users.

### 2.5.1.1 Single Server

Authors in [18] use a central anonymity server through which the mobile users can send queries to LBS. To make the communication between users and the central anonymity server trustful, users set up an encrypted connection with the anonymity server at the beginning. Users sends their encrypted queries to the anonymity server, so that the anonymity server is the only one who can learn the information in the query. The anonymity server decrypts the queries and uses a cloaking algorithm to perturb the position information in the queries. Then the anonymity server sends the modified queries to external services (e.g., LBS). This is a typical centralized protocol, which can reduce the re-identification risk for the users. Its drawback is that a continuous connection to the server is necessary for each user, which is hard to achieve in a sparse DTN. We cannot also assume that a MANET user can have a stable connection with a central anonymity server either.

In [19], researchers employ a matchmaker which is used to match users and advertisements, by which users can achieve anonymization of their identities and locations from the matchmaker. The system architecture in [19] is similar to the former [18], while authors in [19] just focus on the advertisement service instead of the “external services” in [18]. The role of the matchmaker is simply matching users and advertisements. Although the functions of the matchmaker in [19] and the central anonymity server in [18] are different, the intermediate trusted three-party servers (i.e., the matchmaker and the central anonymity server) separate users and the application server (e.g., an advertisement server,
LBS server). The architecture in [19] does not require an encryption process, so the attackers can learn the information in the queries. When a large number of queries arrive at the matchmaker in a short time from different users, it helps the matchmaker mix the queries so that attackers can hardly trace the query, but the burden of the users who are near the matchmaker can be heavy.

In [26], researchers use a trusted, third-party location anonymization engine (LAE) that acts as a middle layer between mobile users and the LBS provider, in which exact locations and requests from clients are replaced by a location anonymization engine before they arrive at the LBS provider. Therefore, it appears that the suggest approach is almost like that shown in Figure 2.4. A trusted server is placed between users and the application server, which hides users’ information and offers sufficient information for the application servers to provide acceptable service.

![Figure 2.4: Single Anonymization Server](image)

2.5.1.2 Multiple Servers

The above protocols always use a single anonymization server, while there are other protocols which need multiple infrastructures.

Authors in [17] propose a protocol, called Social-based PRivacy-preserving packet forwardING (SPRING), for vehicular delay-tolerant network. In their work, they employ Roadside Units (RSUs), which are a type of equipment deployed along the roadside, to assist the packet forwarding and achieve conditional privacy preservation. These RSUs are
located at high social intersections, so that vehicles which pass by the RSUs send their messages to the RSUs. The RSUs have sufficient resource so that they can hold the messages for a long time, which decreases the probability of messages being dropped. The messages are forwarded to proper next-hop vehicles when the vehicles pass by the RSUs. Since messages are held by the RSUs for a period, attackers can hardly trace the messages. Besides, a large number of vehicles send many packets to these RSUs, which enables the RSUs to serve as mix servers. The advantage of SPRING is that it improves the delivery success ratio and privacy-protection performance. However, deploying the RSUs is not always feasible.

Another example is the REAL [7], in which researchers use sensor nodes which are scattered throughout the network to provide anonymized locations for users, as shown in Figure 2.5. The whole system area is partitioned into a set of aggregate locations by the sensor nodes, where there are at least $k$ persons. To provide better location-based service, they minimize the areas of aggregate locations. When a user sends a query to the LBS, he uses the location of the sensor nodes which he belongs to, so that the attacker cannot tell the difference between the requester and the other $k - 1$ users in that aggregate location. This is a typical $k$ anonymity algorithm, whose main disadvantage is that it is difficult to deploy the sensor nodes in real-world. Besides, the mix servers and sensor nodes might be more prominent targets than the LBS providers.

![Figure 2.5: REAL [7]](image)
2.5.2 Distributed Protocols

Although centralized protocols also have good performance in their delivery success ratio and privacy-protection in their own field, the MANET is a network without infrastructure. Distributed protocols are more appropriate for applications in MANET. A problem for a distributed protocol is that whether a user can trust others. Authors in [30], [31] and [32] introduce the social tie to determine whether a user is trustful.

In the distributed social based location privacy protocol (SLPD) [30], authors use two phases: the obfuscation phase and the free phase. A query from an original requester always starts in the obfuscation phase and passes through $k$ friends. For example, the original requester sends the query to one of his friend in one hop, then the friend forwards the query to another friend. We call these friends the agents. That process repeats for exactly $k$ times. When the $k^{th}$ friend get the query, he switches the query to the free phase and replaces the sender identity with his own identity, and then sends the query to the destination (e.g., LBS) using any DTN protocol. The LBS then sends the reply to all $k$ friends who are responsible for forwarding the message to the original requester. In this way, attackers can only learn the identity of all $k$ friends instead of the original requester. Since each of these $k$ friends knows the identity of the original requester, the message can be forwarded to the original requestor. Therefore, the attacker can hardly learn the identity of the original requester. The disadvantage of the protocol is that it is hard to encounter a friend in the network, which can decrease the success ratio for the queries. In the protocol, Hybrid and Social-aware Location-Privacy in Opportunistic mobile social networks (HSLPO) [31], authors try to improve the delivery performance by using a stochastic model which uses a Markov model for location predication. The major process is similar to that in SLPD, but an agent can forward the query to a user who is not a friend of the original requester if the user has more chance to deliver the query and a trust value is larger than a threshold. In other words, an agent continuously searches his
surrounding to find the original requester’s friends. If the agent cannot find the original requester’s friend but his own friend, he checks whether his friend has more chance to deliver the query than him using the Markov model. If his friend is more suitable for forwarding, he sends the query to his friend. The performance of HSLPO depends on the Markov model, that is, whether it can predict users’ movement accurately. In real-world, the movement model for people is more complicated than that used in experiments.

Another protocol, called Location Privacy-Aware Forwarding (LPAF) [32], also attempts to improve the performance of SLPD. Both LPAF and SLPD are similar, but LPAF just adds more friends to the protocol. When an agent cannot find a close friend (i.e., their trust value is high), he will try to find other general friends (i.e., their trust values is lower than the close friends). That might be a safety tradeoff, because some ineligible users in SLPD can be chosen as friends based on the additional criteria imposed by LPAF.

In fact, both the HSLPO and LPAF do not successfully address the problem of finding friends as agents. Although we use the friends of friends or set the threshold for friends low, there are only a few users who can be chosen as agents. In LPAF, the identity of the requester is even exposed to someone who is not very trustful.
Chapter 3

Multi-Hop Location-Privacy Protection

3.1 System Model

Our network architecture consists of two main entities: Users and LBS Providers (LBSPs). Due to the introduction of the social network, the users’ social information can be used in obfuscation forwarding process. Based on available information in the social network, the relationship between two users can be considered as friends or strangers. The user who makes a query to an LBSP will be called the original requester while the others are called intermediate users. LBSPs are located in fixed locations and their coordinates are known by all users when users join the network. Attackers are assumed to be able to access LBSPs, and attempt to locate original requesters. We assume that the LBSPs are semi-trusted and the strangers are un-trusted. We also assume that both entities have sufficient resources, like computational capability, storage and battery power.

Since two friends could be a pair of multi-hop neighbors, users can leverage Optimized Link State Routing Protocol [8] to seek friends continuously after entering the network,
so that they can recognize each other and make contact in time. When a user carries an obfuscation phase query, he might send the query to a multi-hop friend through several strangers. In this case, a secure communication is necessary for between them, so that they must send the query encrypted to prevent strangers from learning anything about the query. Each user obtains a pair of asymmetric keys (public and secret key) before he joins the network from a certificate authority using well-regarded techniques, like in [3]. Whenever a user detects a new friend, he sends a request to the friend asking for his public key. In this way, a user can get his friends’ public key when they encounter each other. Even though several strangers can be active in the obfuscation phase, the queries can still be securely sent to the user’s friend.

The relationship strength is often “a hidden effect of nodal profile similarities” [28]. Let $SV_{i,j}$ denote a value of relationship strength which user $i$ determines whether user $j$ is an acceptable friend based on the relationship strength. For every pair of users ($i$ and $j$), we assume that there is an $SV_{i,j}$. If $SV_{i,j}$ is bigger than a specific friend threshold $T_{\text{min}}$, set by the original requester, user $j$ is considered as a friend of user $i$; otherwise, it will be treated as a stranger. The notations used in this chapter and their meanings are shown in Table 3.1.

### 3.2 Details of MHLPP

MHLPP aims to protect the original requester’s ($N_0$’s) location-privacy using an obfuscation path. In other words, a query $q$ which needs to be obfuscated must go through a series of friends after it leaves $N_0$. The whole process includes two parts: the obfuscation phase and the free phase. In the former phase, $q$ is only transmitted among friends, until it is sent to an area called “obfuscation area”. At the end of that phase the last friend $N_f$ replaces all $N_0$’s information by its own and forwards $q$ with an arbitrary DTN forwarding protocol, like the one suggested in [25]. In this case, what attackers can learn from the
Table 3.1: MHLPP Symbols

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meanings</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_0$</td>
<td>the original requester</td>
</tr>
<tr>
<td>$N_i$</td>
<td>if $i &gt; 0$, it denotes the friend chosen by $N_{i-1}$. If $i = 0$, it is $N_0$.</td>
</tr>
<tr>
<td>$N_f$</td>
<td>the last friend who handles the obfuscation query</td>
</tr>
<tr>
<td>$N_d$</td>
<td>the destination or the LBSP</td>
</tr>
<tr>
<td>$K_i$</td>
<td>the public key of $N_i$</td>
</tr>
<tr>
<td>$S_i$</td>
<td>the secret key of $N_i$</td>
</tr>
<tr>
<td>$q$</td>
<td>a query of $N_0$</td>
</tr>
<tr>
<td>$r_q$</td>
<td>the requirement for the query $q$</td>
</tr>
<tr>
<td>$msg$</td>
<td>a message contains $q$ and $r_q$</td>
</tr>
<tr>
<td>$E_{msg_i}$</td>
<td>the encrypted $msg$ using $K_i$</td>
</tr>
<tr>
<td>$S_{id}$</td>
<td>the original requester’s identity</td>
</tr>
<tr>
<td>$D_{id}$</td>
<td>the destination’s identity</td>
</tr>
<tr>
<td>$L_s$</td>
<td>the location of $N_0$ when it sends the query to $N_1$</td>
</tr>
<tr>
<td>$R_p$</td>
<td>the inner radius of the obfuscation area</td>
</tr>
<tr>
<td>$R_s$</td>
<td>the external radius of the obfuscation area</td>
</tr>
<tr>
<td>$T_{min}$</td>
<td>the social value bound for friends</td>
</tr>
<tr>
<td>$C_{max}$</td>
<td>the extra path limit in each obfuscation forward</td>
</tr>
<tr>
<td>$SV_{i,j}$</td>
<td>the relationship strength between user $i$ and $j$</td>
</tr>
</tbody>
</table>

database in LBSP is $N_f$’s information, so they can hardly infer the original requester’s identity and location based on that information. The free phase starts when the query $q$ is forwarded by $N_f$ and ends when it reaches the LBSP.

Because $N_f$ is the only identity the LBSP knows, the LBSP has no choice other than replying to the last friend $N_f$ when it receives the obfuscated query. The reply can be delivered with an arbitrary DTN routing protocol as the free phase query does. The friend $N_f$ should remember who is the real destination ($N_0$) of this reply, then he transmits it to $N_0$. In this way, $N_0$ is able to send a query $q$ to an LBSP while not exposing his own information.

The obfuscation phase of a query $q$ starts when the query leaves the original requester $N_0$. When a user is holding an obfuscation phase query, he starts sensing connected friends continuously, which enables it to communicate with one-hop or multi-hop neighbor friends. Even though users in the mobile network use OLSR protocol [8] to detect others
automatically, they do not communicate with their friend unless they have a requirement to send an obfuscation query. Also, they do not ask their friends for public keys. Therefore, carrying an obfuscation phase query requires a user to execute MHLPP algorithm.

When $N_0$ finds the first available friend $N_1$, he asks $N_1$ for a public key $K_1$, which will enable him to encrypt his query using $K_1$. That prevent others, e.g. strangers, from learning information in the message $msg$ that that contains both $q$ and $r_q$. $r_q$ is $N_0$’s requirement for $q$, which is always sent with the query $q$ and remains constant until the end of the obfuscation phase (we discuss this in section 3.3). Friends who get the query can infer $q$’s obfuscation area based on parameters $R_p$, $R_s$ and $L_s$ in $r_q$, which is a ring with inner radius $R_p$, external radius $R_s$ and center $L_s$. Before $N_0$ sends the query $q$ to his friend, he initializes parameter $L_s$ to his current location and encrypts $msg$ using $K_1$ to get $E_{msg_1}$ which is what $N_0$ sends to $N_1$.

The destination of $E_{msg_1}$ is $N_1$, which is a plaintext in $E_{msg_1}$, so that other intermediate users (strangers) can help $N_0$ forward $E_{msg_1}$ to $N_1$. In this step, strangers transmit $E_{msg_1}$ using the OLSR protocol if $N_1$ is a multi-hop neighbor of $N_0$. Strangers learn nothing other than the identity of $N_1$, because both $q$ and $r_q$ are encrypted. They cannot help attackers locate $N_0$ because they do not know $S_{id}$ (the identity of $N_0$) and $D_{id}$ (the LBSP) included in $r_q$.

When $N_1$ receives $E_{msg_1}$, he decrypts it with its secret key $S_1$ to get $q$ and $r_q$. If $q$ is already in the obfuscation area defined in $r_q$ (i.e., it is already in the ring), the query $q$ finishes its the obfuscation phase. Then $N_1$ replaces all information of $N_0$ with his own. For example, the $S_{id}$ is replaced with $N_1$. If a location is necessary for the LBS, $N_1$ uses his own current location and records this change in his memory before initiating the free phase. A free phase query can then be forwarded to the destination (i.e., LBSP).

If $q$ is still in the obfuscation phase (not in the ring), $N_1$ performs similar actions just as $N_0$ expect modifying $r_q$. Another difference is that instead of finding friend randomly,
would seek for a friend who is nearer in the obfuscation area, and so will the following friend.

The detailed algorithm is explained in Algorithm 3.1 where \( N_x \) is a neighbor of \( N_i \) who is carrying the query \( q \). Procedure \textit{"DealWithQuery"} is responsible for dealing with a query. For \( N_0 \), he generates the query \( q \) and its requirement \( r_q \). If \( N_i \) receives \( Emsg_i \), he decrypts it with his own secret key \( S_i \). If \( q \) finished its obfuscation phase at \( N_i \), \( q \) will be required to be forwarded in free phase immediately. Otherwise, \( q \) needs to be processed in the obfuscation process. Both \( q \) and \( r_q \) are stored in \( N_i \) until they are sent to the next friend. \( N_i \) starts detecting friends continuously if and only if \( N_i \) carries one or more obfuscation phase queries.

When \( N_i \) detects a new neighbor \( N_x \) (one-hop or multi-hop neighbor), he follows steps in \textit{"WhenEncounterUser"}. For an expired query, \( N_i \) simply drops it. If the query \( q \) is already inside its obfuscation area, \( N_i \) switches it to the free phase. If \( q \) stays in the obfuscation phase and \( N_x \) is an available friend, \( N_i \) encrypts both \( q \) and \( r_q \) using \( N_x \)’s public key \( K_x \) to get an encrypted message \( Emsg_x \). Then \( N_i \) forwards \( Emsg_x \) to \( N_x \) and stops sensing friends after \( Emsg_x \) departs from it.

When we mention that \( N_i \) switches a query \( q \) to the free phase, \( N_i \) actually replaces \( N_0 \)’s information with its own one in \( q \) to get \( q^* \) and records this replacement in its storage, then \( N_i \) uses the Spray and Wait protocol [25] to forward \( q^* \) in plaintext. That allows \( N_i \) to hide \( N_0 \)’s identity and forward a reply from LBSP to \( N_0 \).

### 3.3 Requirement parameters

In the obfuscation phase, \( r_q \) is always in \( msg \) so that friends who get \( msg \) can make decisions (e.g. selections of friends) based on it.

All parameters (i.e., \( S_{id}, D_{id}, R_p, R_s, L_s, T_{min} \) and \( C_{max} \)) in \( r_q \) are given by \( N_0 \) before
Algorithm 3.1 The Obfuscation Phase in MHLPP

1: procedure DEALWITHQUERY
2: if the current user is \( N_0 \) then
3: \( (q, r_q) \) by himself
4: else
5: if the current user is \( N_i, i > 0 \) then
6: \( (q, r_q) \leftarrow Decrypt_{S_i}(Emsg_i) \)
7: end if
8: end if
9: if \( q \) can switch to the free phase based on \( r_q \) then
10: SwitchFree\( (q) \)
11: else
12: \( msg \leftarrow (q, r_q) \)
13: Store \( msg \)
14: Start sensing friends
15: end if
16: end procedure

17: procedure WHENENCOUNTERUSER(\( N_x \))
18: \( q \leftarrow \) get query from \( msg \), \( r_q \leftarrow \) get requirement from \( msg \)
19: if \( q \) timeout then
20: remove \( msg \) return
21: end if
22: if \( q \) is eligible to switch into the free phase then
23: SwitchFree\( (q) \) return
24: end if
25: if \( SV_{i,x} \) is bigger than \( T_{\text{min}} \) in \( r_q \) then
26: if it is the first hop of \( q \) then
27: assign the current location to \( L_s \) of \( r_q \)
28: end if
29: \( Emsg_x \leftarrow Encrypt_{S_x}(q, r_q) \)
30: forward \( Emsg_x \) to \( N_x \)
31: remove \( msg \) from memory
32: stop sensing friends
33: end if
34: end procedure

35: procedure SWITCHFREE\( (q) \)
36: \( q^* \leftarrow \) replace \( q \)‘s requester-information \( (N_0) \) by \( N_i \)
37: record \( (q, q^*) \)
38: forward \( q^* \) with DTN protocols
39: end procedure
leaves \( N_0 \). Parameters \( S_{id} \) and \( D_{id} \) record the identities of \( N_0 \) and the destination (LBSP) \( N_d \), based on which last friend \( N_f \) is able to send the query freely to \( D_{id} (N_d) \) and forward the reply to \( S_{id} (N_0) \).

The obfuscation area is a ring with an inner radius \( R_p \) and an external radius \( R_s \). As shown in Figure 3.1(a), the obfuscation area is actually the grey area “a”. obfuscation area must guarantee both the original requester’s location-privacy and location awareness. In other words, the value of \( R_p \) should be big enough, so that there are sufficient users in the inner circle (with a radius \( R_p \)). At the same time, \( R_s \) should be small enough so that the LBSP can provide a service, acceptable to \( N_0 \).

![Diagram](image)

(a) The Ring  
(b) The Agent And The Destination

Figure 3.1: The Selection Of The Next Friend

A user \( N_x \) can be chosen by \( N_i \) as a friend for \( q \) if and only if \( SV_{i,x} \) is bigger than the threshold \( T_{min} \). The original requester \( N_0 \) can set various values for his queries based on their importance. If \( T_{min} \) is large, there would be fewer friends for any users in the network which reduces the query success rate to a certain extent, as a result. We assume that the original requester can balance the level of privacy and the success ratio.

Most DTN routing protocols aim to deliver queries through the shortest path, while MHLPP pays more attention to security in its obfuscation phase. Consequently, the obfuscation process in MHLPP results in a longer path from the original requester \( N_0 \) to the
destination $N_d$. To limit the length of the path, we introduce parameter $C_{max}$ which is the maximum extra path (e.g., the difference of the length and the distance between the $N_i$ and LBSP) we can tolerate. For any friend $N_i$ who gets a $C_{max}$ from $r_q$, if he selects $N_x$ as the next friend, the extra path should not be longer than $C_{max}$. Let’s denote the optimal path from user $m$ to $n$ by $Dis(m, n)$, and the extra path from $N_i$ to $N_d$ through $N_x$ by $C_{i,x,d}$. Then $C_{i,x,d}$ can be defined as follow.

$$C_{i,x,d} = Dis(i, x) + Dis(x, d) - Dis(i, d)$$  (3.1)

$C_{i,x,d}$ must be a value smaller than $C_{max}$. If $Dis(m, n)$ is the straight-line distance between point $m$ and $n$, then next friend $N_x$ should be in an ellipse $E_C$ with focus points $N_i$ and $N_d$. Let’s denote the coordinate of $N_i$ by $(-\frac{d}{2}, 0)$ and the coordinate of $N_d$ by $(\frac{d}{2}, 0)$. Then, the equation of the ellipse $E_C$ is

$$\frac{x^2}{(d + C_{max})^2} + \frac{y^2}{2d \cdot C_{max} + C_{max}^2} = \frac{1}{4}$$  (3.2)

As shown in Figure 3.1(a), $L_s$ is the center of the ring while $R_p$ and $R_s$ are the inner and external radii, respectively. The query $q$ switches to the free phase when it enters the ring area.

As shown in Figure 3.1(b), $N_i$ who is carrying obfuscation queries should choose his next friend $N_x$ in the ellipse, which avoids the query $q$ going through an unacceptably long path.

In conclusion, a query $q$ starts at the center and moves inside the ring, until it reaches the obfuscation area. The point $N_i$ in Figure 3.1(b) should be inside the ring, and the point $N_d$ might be anywhere. As a result, a user $N_i$ who is carrying an obfuscation query detects a friend continuously who has a larger distance from $L_s$ and inside an ellipse. If there is a friend like that, $N_i$ sends the query to that friend $N_x$. 
3.4 Privacy Analysis

We assume that attackers can achieve all information in LBSPs know. Obviously, they can know the identity of the last friend $N_f$ who replaces $N_0$’s information with his own. It is possible for the attackers to locate $N_f$ with little cost. For example, if $N_0$ stops moving after sending the query $q$, it is reasonable for $N_f$ to believe that $N_0$ is in a ring centered at the location of itself with radii $R_p$ and $R_s$. In other words, the distance between $N_f$ and $N_0$ should be in a range between $R_p$ and $R_s$. If attackers find all users who satisfy this condition, the original requester might be among these users with high probability. Then, a success ratio $P_{r_p r_s}$ to locate $N_0$ can be measured by a conditional probability

$$P_{r_p r_s} = p_{r_p r_s} \cdot \frac{1}{m_{r_p r_s}}$$  \hspace{1cm} (3.3)

where $P_{r_p r_s}$ is the probability that $N_0$ is in the ring (i.e., the distance between $N_0$ and $N_f$ is larger than $R_p$ and smaller than $R_s$). Here, $m_{r_p r_s}$ is the number of users who are in the ring. Attackers locate $N_0$ successfully if and only if $N_0$ is in the ring, at the same time, attackers pick the correct one from all $m_{r_p r_s}$ users at that area.

In the worst case, attackers know exact values $R_s$ and $R_p$. Then, the Eqn. (3.3) becomes

$$P_{R_p R_s} = p_{R_p R_s} \cdot \frac{1}{m_{R_p R_s}}$$  \hspace{1cm} (3.4)

where $P_{r_p r_s}$ is the probability that $N_0$ is on the ring (i.e., the distance between $N_0$ and $N_f$ is larger than $R_p$ and smaller than $R_s$). $m_{r_p r_s}$ is the number of users who are in the ring. Since parameters (e.g., $R_p$ and $R_s$) in $r_q$ are kept secret among trusted friends in our system model, attackers can hardly get the actual values of those parameters.
### 3.5 Complexity discussion

In order to guarantee secure communications among friends, encryption is introduced in our protocol. In the obfuscation phase, the query is transmitted along friends, i.e., $N_0, N_1, N_2, ..., N_f$. When the query is sent from $N_i$ to $N_{i+1}$, a pair of encryption and decryption is needed, so the number of such pairs $T_{en}$ should be equal to $f$.

$T_{en}$ grows with both $T_{min}$ (threshold used to decide friend relationship) and inner radius $R_p$. Essentially, it is the number of friends participating in transmitting a query $q$ in its obfuscation phase that influences $T_{en}$. Given a smaller $T_{min}$, a user carrying the obfuscation phase query has more chances to encounter more friends in a certain area. A larger $R_p$ also leads to a bigger area inside the ring, so that there are more friends in this area. We evaluate the number of encryptions and decryptions in our simulation. Figure 3.2 shows the average number of encryptions ($T_{en}$) with different friend thresholds $T_{min}$ and inner radius $R_p$. We observe that $T_{en}$ increases steadily as we increase $T_{min}$ (i.e., 85%, 90%, and 95%) and $R_p$ (i.e., the horizontal axis).

![Figure 3.2: The Number Of Encryption With Various Inner Radius](image)

It is evident that encryption and decryption process in MHLPP results in an extra cost
in both energy and computational resources. However, the number of encryptions and decryptions is quite low (below 3) which reasonable based on the experiment.

### 3.6 Performance Analysis

We use the map of Helsinki in our simulator to evaluate MHLPP. It is also compared against the known protocol, Hybrid and Social-aware Location-Privacy in Opportunistic mobile social networks (HSLPO). The simulation parameters are shown in Table 3.2. All pedestrians and cars are users in MHLPP. These users are moving on the map along streets continuously. There is an LBSP fixed at a random location on the map. For each user, we give him random social values between 0% and 100%, each corresponding to all other users. Each value has the same probability, so we can compute the expected number of friends of a user. For example, if we are given a privacy threshold ($T_{min}$) of 85%, then there might be 15% (100%-85%) users who are friends of a certain user.

As shown in Table 3.2, there are 126 users in the map, just like what authors of SLPD did. For each of them, say user $i$, we give him 126 random $SV$ values, which denotes the relationship strength between him and other users, so that there are $126^2$ $SV$s in our simulation. The $SV$s are between 0 and 100. As a result, if the $T_{min}$ is equal to 85, the average number of friends of each user should be $18.9 (=126 \times (100 - 85)/100)$.

#### Table 3.2: MHLPP Experiment Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simulation Time</td>
<td>10 minutes</td>
</tr>
<tr>
<td>Map Size (W x H)</td>
<td>4500 m x 3400 m</td>
</tr>
<tr>
<td>Total number of users</td>
<td>126</td>
</tr>
<tr>
<td>Pedestrians/ Cars</td>
<td>84/42</td>
</tr>
<tr>
<td>Communication Area Radius</td>
<td>10m – 90 m</td>
</tr>
<tr>
<td>Pedestrian Speed</td>
<td>1.8-5.4 Km/h</td>
</tr>
<tr>
<td>Car Speed</td>
<td>10-50 Km/h</td>
</tr>
</tbody>
</table>

Users are placed at random locations at the beginning of each experiment. We choose
another random point for each user, so that he can move back and forth along streets between that point and the point his starts at. The user speed depends on the user’s type (pedestrians or cars) and is set randomly. All queries have a 10-minute timeout. The queries which are expired before they reach the LBSP (the destination) are considered to be failed in our success ratio statistics.

In the following experiments, we select 100 users randomly each time, and each selected user sends a query to the destination so that there are 100 queries sent to the destination. We count the number of queries received by the destination in 20 minutes and calculate the query success ratio. If LBS receives 75 queries, then the query success ratio is 75%. One group of parameters (e.g., the communication range, the privacy threshold, and $k$) is in correspondence to one scenario and we process 100 times of trials for each scenario. The experiment result of each scenario we show comes from the average of its corresponding 100 trials.

Figures 3.3-3.5 compare performances between HSLPO and MHLPP for different values of $k$, communication radius and privacy threshold ($T_{\text{min}}$ in MHLPP). The $k$ is the privacy-level requirement in HSLPO. Both HSLPO and MHLPP have different criteria in which a query can switch to the free phase. To make them comparable, we create a new parameter, called *obfuscation distance*. If a query leaves $N_0$ at location $L_a$ and switches to the free phase at $N_f$ whose location is $L_b$, then the obfuscation distance is the straight-line distance between $L_a$ and $L_b$. We test the obfuscation distances of HSLPO with different parameters, and then we set the inner radius of MHLPP to those values. The query success ratio is the ratio of delivered queries to the total number of queries. The number of hops ($h$) is the number of intermediate users between $N_0$ and the destination (LBSP). We count the number of users surrounding the last friend in a specific range, which is $k$ times the communication radius. We calculate the entropy using the reciprocal of the number of surrounding users.
3.6.1 Query success ratio

The query success ratio is the percentage of delivered queries among a number of attempts. Based on the timeout value in Table 3.2, a query is delivered successfully, if it arrives at the LBSP (the destination) before the timeout; otherwise it fails. We use the query success ratio to evaluate the delivery performance of MHLPP.
Figure 3.3: The Query Success Ratio Comparison Between HSLPO and MHLPP

(a) Query Success Ratio Versus Various $k$

(b) Query Success Ratio Versus Various Communication Radius

(c) Query Success Ratio Versus Various Privacy Thresholds
As shown in Figure 3.3(a), the success ratio in MHLPP is always higher than that in HSLPO. As the value of \( k \) increases, HSLPO success ratio drops sharply while MHLPP remains stable. This is because the larger \( k \) is, the harder it is for HSLPO to find enough friends in a limited time. The lack of friends has less impact on MHLPP. We observe that the success ratio of MHLPP rises when \( k = 7 \). That is because it depends on the inner radius which is equal to the obfuscation distance of HSLPO. The obfuscation distance decreases when \( k = 7 \), because most of the queries which complete their obfuscation phase have a short obfuscation distance. In Figure 3.3(b), both HSLPO and MSLPP values increase and have the same trend when given a larger communication radius. The reason is that the communication radius effects the free phase more than the obfuscation phase for both. As shown in Figure 3.3(c), higher privacy threshold leads to lower success ratio in two algorithms. Its impact on HSLPO is more intense than that on MHLPP, which is the most important characteristic of MHLPP. MHLPP has a better performance than HSLPO especially when there are fewer friends in the network. MHLPP can transmit messages with the help from strangers in its obfuscation phase while HSLPO cannot.

### 3.6.2 Number of Hops

We count the number of hops it takes for queries to be delivered successfully and calculate the average. Every user who takes part in the delivery process is considered in the hop count. We introduce this criterion to measure the routing path length of the algorithm. MHLPP is more sensitive to the probability that a user encounters a friend than HSLPO is. The reason is that MHLPP aims to reach a certain distance rather than taking certain number of hops. In other words, MHLPP continues sending queries to other friends until queries enter their obfuscation area. In this process, MHLPP takes every chance to forward queries. If it is hard for MHLPP to find friends, it can also take the queries to obfuscation areas with fewer friends. Therefore, the probability that users encounter friends has less impact on the performance of MHLPP. The result is shown in Figure 3.4.
Figure 3.4: The Number Of Hops Comparison Between HSLPO And MHLPP

(a) Number Of Hops With Various $k$

(b) Number Of Hops With Various Communication Radii

(c) Number Of Hops With Various Privacy Thresholds
In Figure 3.4(a), the number of hops in HSLPO is affected by parameter \( k \) obviously. Especially, the first \( k \) hops forwarders must be friends, which makes it hard for HSLPO to have queries to be forwarded successfully. Both protocols have similar number of hops in their free phases, but HSLPO has exactly \( k \) hops in its obfuscation phase, while MHLPP can have fewer than \( k \) hops. In figure 3.4(b), the number of hops in MHLPP grows with the communication radius obviously, while it does not change a lot in HSLPO, because only successful delivery queries are counted in the statistics. Given a large communication radius, MHLPP has a much higher success ratio for delivered queries as it can connect more friends. In Figure 3.4(c), the value of MHLPP drops for higher privacy thresholds. The reason is the same as Figure 3.4(b). For HSLPO, no matter how hard it is to find a friend, it attempts to find exactly \( k \) friends. However, if it is too hard to find a friend, MHLPP’s friend can carry the query while moving and complete the obfuscation process. For higher privacy thresholds (i.e., resulting in fewer friends), MHLPP chooses to carry queries other than finding friends. That results in a drop in the number of hops.

### 3.6.3 Security

Since the principles with that two protocols protect original requesters are different, we evaluate the probability that attackers locate the original requester if the distance between him and the last friend is smaller than a some value \( r \), which is equal to \( k \) times the communication radius. Since the last friend reveals himself to the LBSP, attackers might locate him accurately. We assume that attackers know the privacy parameter \( k \). In the worst case, the distance between the original requester and the last friend is smaller than \( r \) when attackers start to locate the original requester. That gives attackers a chance to locate the original requester. We count all users who are inside the radius \( r \) of the last friend, and the original requester is one of them. For example, if there are \( m \) users in the area, the probability should be \( \frac{1}{m} \). Figure 3.5 compares the entropy \( E \) of both HSLPO and
MHLPP. We use the following formula for computing entropy:

\[ E = -\frac{1}{m} \log_2 \left( \frac{1}{m} \right) \]  

(3.5)

From Figure 3.5(a), we observe that MHLPP has very small (about 0.04) increase in entropy compared to HSLPO. When the original requester is in the circle centered at the last friend, HSLPO is a little more secure than MHLPP but not by very much. That is because HSLPO always switches to the free phase when the last friend encounters the previous friend, so the previous friend must in the circle. MHLPP does not have this condition. Both graphs in Figure 3.5(a) and Figure 3.5(b) have the same trend. The curve of MHLPP is also a little higher than that of HSLPO, while two curves almost meet when the communication radius is small or large. Given a small radius, the entropy of both protocols are small. When the radius is large, we can ignore the effect of the previous friend mentioned about for Figure 3.5(a) as there are so many users in the circle. From Figure 3.5(c), since the circle neither expands or shrinks, we observe that the two curves exhibit similar behavior. The values of HSLPO are always lower than the correlated values of MHLPP. However, as we observed in the experiment, the last friend is always hundreds of meters away from the requester.
Figure 3.5: Locating Probability Entropy Comparison Between HSLPO And MHLPP

(a) Locating Probability Entropy With Various $k$

(b) Locating Probability Entropy With Various Communication Radii

(c) Locating Probability Entropy With Various Privacy Thresholds
Chapter 4

Appointment Card Protocol

4.1 System Model

The network architecture consists of two main classes of entities: Users and Location-Based Service Providers (LBSPs). Users are mobile and communicate with other users and LBSPs within a certain range, i.e., the communication range of their portable devices. For a given user, other users in the social network are either strangers or his friends whom he can detect when they are in his communication range. Let $RS_{i,j}$ denote the relationship strength between user $i$ and $j$. If $RS_{i,j}$ is larger than a specific threshold, $FT_{min}$, user $j$ is considered a friend of $i$. LBSPs, which provide location-based services to the users are fixed and not part of the social network. We assume that the only information which is necessary for the LBSP is a location from the original requester, but the original requester should still give an identity (not his own) to the LBSP so that the LBSP can reply to that identity.

We consider external attacker capable of eavesdropping on limited traffic in the network. We assume that the attacker can access the database of LBSPs, so that he can learn everything recorded in LBSP’s memory, including user identities and locations. The attacker launches an inference attack on each user who uses the LBS in an attempt to learn
user’s private information based on location and context in the queries. Therefore, the key to protecting location-privacy is degrading the relationship between the user identity and the location provided by him so that the attacker can hardly infer the identity of the original requester by the known information.

We propose a protocol, called Appointment Card Protocol (ACP), to protect the identity and location-privacy of the original requester by providing other users’ identity (agents), which can be any user in the network so that ACP can have a large anonymity set. The friends of the original requester separate the agents and the original requester so that the agents have no knowledge about the original requester.

4.2 Appointment Card Protocol Overview

Our proposed ACP protects original requesters when they are served by LBSPs. Every user generates Appointment Cards (ACs) containing his own identity called $Cid$ and a unique number $Capt$ which is generated by himself, and he is the first agent ($Agt_1$) of ACs generated by himself. The ACs are exchanged when two users encounter each other. The user who gets the ACs from $Agt_1$ becomes the second agent ($Agt_2$) of the ACs. More users become the ACs’ agents when they get the ACs, and each AC must have $k$ agents before a user can use it in a query. When the original requester sends a query, he chooses an AC and sends the query using the identity $Agt_1$ which is in the AC. The LBSP replies to $Agt_1$ when it receives the query. $Agt_1$ then forwards the reply to the next agent (i.e., $Agt_2$), and so on until the reply reaches the last agent ($Agt_k$). $Agt_k$ is responsible for forwarding it to the original requester. Therefore, we can consider the ACP having two parts: 1) users generate and exchange ACs continuously; 2) users use ACs when they want to send a query.
Figure 4.1 is an example of the execution of the ACP protocol. Explanations of the symbols in the figure are shown in Table 4.1. These symbols and the figure are used throughout the chapter to help us describe the protocol. For simplicity, we will omit some superscripts and subscripts from these symbols in the following sections when there is no ambiguity. The whole process can be considered as the following parts: 1) exchanging cards among all users who are called agents (i.e., 1 and 2), 2) exchanging cards among friends (i.e., 3), 3) sending the query using information of ACs (i.e., 4), 4) forwarding the reply among agents (i.e., 5, 6 and 7), and 5) relaying to the original requester (i.e., 8).
### Table 4.1: ACP Symbols

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meanings</th>
</tr>
</thead>
<tbody>
<tr>
<td>$U_\varepsilon$</td>
<td>An user whose identity is $\varepsilon$.</td>
</tr>
<tr>
<td>$AC^\beta_\alpha$</td>
<td>The $\beta^{th}$ appointment card generated by user $\alpha$.</td>
</tr>
<tr>
<td>$AC^\beta_{\alpha,\gamma}$</td>
<td>$AC^\beta_\alpha$ is being forwarded by user $\gamma$ who is an agent.</td>
</tr>
<tr>
<td>Query$^\alpha_{\delta(\beta)}$</td>
<td>A query whose original requester is $\delta$ and using $AC^\beta_\alpha$.</td>
</tr>
<tr>
<td>Reply$^\alpha_{\beta}$</td>
<td>The reply of a query which uses $AC^\beta_\alpha$.</td>
</tr>
<tr>
<td>Reply$^\alpha_{\gamma,\beta}$</td>
<td>Reply$^\alpha_{\beta}$ is being forwarded by user $\gamma$ who is an agent.</td>
</tr>
<tr>
<td>Agt$^i_{\alpha(\beta)}$</td>
<td>The $i^{th}$ ($i \geq 1$) agent of $AC^\beta_\alpha$.</td>
</tr>
<tr>
<td>capt$^\beta_\alpha$</td>
<td>The parameter Capt in $AC^\beta_\alpha$. see Table 4.2</td>
</tr>
<tr>
<td>aapt$^\alpha_{\gamma,\beta}$</td>
<td>The parameter Aapt in $AC^\beta_\alpha$, which is given by user $\gamma$ who is an agent. see Table 4.2</td>
</tr>
<tr>
<td>AN</td>
<td>Both the Capt and the Aapt in an AC are called the Appointment Number.</td>
</tr>
<tr>
<td>NR$^\varepsilon$</td>
<td>The number of ready-ACs carried by $U_\varepsilon$.</td>
</tr>
</tbody>
</table>
4.3 Appointment Card

To protect the original requester’s location privacy, the original requester uses others’ identity (i.e., $Agt_1$) to send queries to the LBSP instead of his own identity, so that the LBSP can reply to the original requester through $Agt_1$. ACs make it possible for the agents to forward the reply to the original requester. In other words, An AC indicates a path through which the original requester can get his reply.

In Figure 4.1, $U_a$, $U_b$, and $U_c$ are the agents of $AC^{β}_a$ (i.e., $Agt^{α(β)}_1$, $Agt^{α(β)}_2$ and $Agt^{α(β)}_3$). These agents are strangers, so the attackers can hardly infer $U_c$ from the identity of $U_a$. At the same time, $U_c$ is in the original requester $U_d$’s social tie (i.e., $U_c$ is $U_d$’s friend or his friends’ friend, so on), and he is the only one who knows how to reach $U_d$. Therefore, it is hard for attackers to infer the identity of $U_d$ from the identity of $U_a$.

Notice that $U_c$ receives $AC^{β}_a$ from a stranger $U_b$ who knows the information of $AC^{β}_a$ and the identity of the next agent $U_c$, so that it is unsafe for $U_c$ to use $AC^{β}_a$. In other words, $AC^{β}_a$ cannot be used until $U_c$ gives it to another user (e.g., the user $d$) who trusts $U_c$. The AC is called a ready appointment card (simply ready-AC) after it leaves the last agent (i.e., $U_c$), or it is called the distributing appointment card (simply distributing-AC). It is obvious that distributing-ACs are transmitted among agents who can be strangers, while an user can only get ready-ACs from one of his friends.

To make users carry a similar number of ready-ACs, ready-ACs are also exchanged between friends, so that an user can get ready-ACs from his friends who have more ready-ACs than him. As a result, the last agent is not sure whether the user who gets the ready-AC from him is the original requester. We introduce a pseudonym mechanism which enables the last agent to forward the reply to the unknown original requester.

All users in the network are responsible for generating their respective ACs, and they are called the creators of their own ACs. The creator records his own identity ($Cid$) and a unique number ($Capt$) on his AC. When users exchange ACs, they modify $Aid$ (the agent
ID) and \( Aapt \) (the agent’s appointment number) in the AC to enable the next agent to identify who is the predecessor. Entries of ACs are shown in Table 4.2.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meanings</th>
</tr>
</thead>
<tbody>
<tr>
<td>( Cid )</td>
<td>The identity of the creator who generates the AC.</td>
</tr>
<tr>
<td>( Capt )</td>
<td>A unique number that distinguishes an AC from other ones generated by the same creator.</td>
</tr>
<tr>
<td>( Aid )</td>
<td>The identity of an agent who gives the AC to the recent holder. (The previous hop of the AC)</td>
</tr>
<tr>
<td>( Aapt )</td>
<td>A unique number that distinguishes an AC from other ones transmitted by the same agent.</td>
</tr>
<tr>
<td>( Timeout )</td>
<td>The time when the AC expires.</td>
</tr>
<tr>
<td>( EQ)</td>
<td>A queue (Exchange Queue) which records the AC’s agents in order. Its length is ( EQL ).</td>
</tr>
</tbody>
</table>

### 4.4 AC Life Cycle

The life cycle of an AC starts when it is generated by its creator. The first \( k \) (see Table 4.3) agents add their identities into its Exchange Queue (\( EQ \)) (see Table 4.2) before exchanging it, which increases the length (\( EQL \)) of the \( EQ \). When the AC’s \( EQL \) reaches \( k \), it is eligible to be used in a query and is called a ready-AC. When an AC is used in a query, it is marked as an used AC by the original requester who uses the AC. An AC starts at the distributing state. No matter what state (distributing, ready or used) an AC is in, it can expire, as shown in Figure 4.2. If the length of its \( EQ \) reaches \( k \), it is switched to the ready state. When an user uses a ready-AC in a query, the AC is switched to the used state. The user can also use the used-AC in other queries but he does not give the used-AC to anyone else.
4.5 System Parameters

All the system parameters are shown in Table 4.3.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meanings</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k )</td>
<td>The obfuscation distance</td>
</tr>
<tr>
<td>( m )</td>
<td>The friend obfuscation distance</td>
</tr>
<tr>
<td>( GP )</td>
<td>The generating period of ACs</td>
</tr>
<tr>
<td>( Seg )</td>
<td>The distributing segment</td>
</tr>
<tr>
<td>( \tau  )</td>
<td>Avoiding time</td>
</tr>
<tr>
<td>( AT )</td>
<td>The timeout for ACs</td>
</tr>
</tbody>
</table>

4.5.1 Obfuscation Distance

The obfuscation distance \( k \) is the number of exchange before an AC is switched to the *ready* state. In other words, an AC must be exchanged \( k \) times before it becomes a *ready*-AC which can be used by an user in queries.

As shown in Figure 4.3, the \( k \) agents are strangers so that the only relationship between two adjacent ones is that they encounter each other somewhere. The relationship between \( Agt_1 \) and \( Agt_k \) becomes weaker when we increase \( k \). In other words, attackers can hardly
inference the identity of $Agt_k$ when they only know the identity of $Agt_1$, and the difficulty increases with the increase of parameter $k$. As a result, it is hard for attackers to infer the identity of the original requester, even though $Agt_k$ is in the social tie of the original requester. Since the reply message must go through a series of agents, a long obfuscation distance also lengthens the path of the reply message. Therefore, a large $k$ makes the original requester safer, while making it harder and longer for the reply to be delivered.

![Figure 4.3: Obfuscation Distance](image)

### 4.5.2 Friends Obfuscation Distance

Since $Agt_{k-1}$ is a stranger for $Agt_k$, it is possible that $Agt_{k-1}$ is the attacker. We assume that the attacker knows that $Agt_k$ is in the social tie of the original requester. The attacker can assume that $Agt_k$ is a close friend of the original requester, so the identity of $Agt_k$ gives the attacker a good tip to infer the original requester. A solution to prevent the agent $Agt_{k-1}$ from learning the identity of the original requester easily is that the last $m$ ($1 \leq m \leq k$) agents are friends, as shown in Figure 4.4. Here, $m$ is called *friends obfuscation distance*, and the last $m$ agents are trusted agents.

It is true that $Agt_i$ is a friend of $Agt_{i+1}$, $i > k - m$, but two nonadjacent trusted agents (e.g., $Agt_i$ and $Agt_{i+2}$) might have a weak relationship. Since there are at least $m$ trusted agents between the stranger $Agt_{k-m}$ and the original requester, $Agt_{k-m}$ can hardly infer the identity of the original requester based on information he learns. When $m = k$, all ACs must be exchanged between friends only. When $m = 1$, the last agent is the only one
who is in social tie of the original requester, which is the case in our example.

However, friends encounter each other rarely, so having a large $m$ increases the difficulty of distributing ACs. In this work, we assign $m$ to 1.

### 4.5.3 Generating Period

Since ACs could expire, users must generate new ACs continuously. We use $GP$ to denote the speed of generating new ACs per user; that is, each user generates a new AC every $GP$ seconds.

### 4.5.4 Distributing Segment

It is the series of random agents that increases the difficulty for attackers to infer the identity of the original requester. However, it is possible that many ACs are transmitted by the same series of agents. We use the system parameter distributing segment, $Seg$, to avoid giving all distributing-ACs to the same user. Each user maintains $Seg$ number of Distributing AC Lists ($DLs$) and puts received distributing-ACs in one of those $DLs$ randomly. If $Agt_i$ exchanges ACs with another user, $Agt_i$ selects one of his $DLs$, and only ACs in that $DL$ will be given to that user.

In our example Figure 4.1, we assume that $Seg$ is equal to two so that each user has two $DLs$ (i.e., $DL1$ and $DL2$). When $U_b$ receives $AC^{1}_{a,a}$, $AC^{2}_{a,a}$ and $AC^{3}_{a,a}$ from $U_a$, $U_b$ may

![Figure 4.4: Friends-Obfuscation Distance](image)
put $AC_{a,a}^{1}$ and $AC_{a,a}^{2}$ in its DL1, while $AC_{a,a}^{3}$ in its DL2. If $U_b$ encounters $U_c$, $U_b$ can give either $AC_{a,b}^{1}$ and $AC_{a,b}^{2}$ or only $AC_{a,b}^{3}$ to $U_c$. In this way, we separate the ACs generated by the same creator $U_a$.

### 4.5.5 Avoiding Time

It makes the obfuscation path of an AC simpler that the AC has duplicate agents, which facilitate attackers’ inference about the identity of the original requester. We use a parameter avoiding time, $\tau$, to optimize the agent selection strategy. If an user gets an distributing-AC at time $t_i$, he cannot get that distributing-AC again before time $t_i + \tau$.

For example, we assume that two users, e.g., $U_A$ and $U_B$, are walking together for a period. Also assume that $U_A$ generates an AC (e.g., $AC_A$) at $t_0$ and gives it to $U_B$, then $AC_A$ is given back to $A$ and so on. The distributing phase of the AC only costs a few seconds, because $U_A$ and $U_B$ exchange $AC_A$ time and again, but they are the only agents involved. The above scenario defeats the purpose of exchanging ACs because it is easy for an attacker to infer the identity of the last agent ($U_A$ or $U_B$) from the first agent $U_A$. We can prevent an AC from having duplicate agents when using the parameter $\tau$. For example, $U_B$ receives a certain AC $AC_A$ from $U_A$ at $t_0$, then $U_B$ sends it to an user C ($U_C$) who can also send it to others. If an user carrying $AC_A$ encounters $U_B$ before $t_0 + \tau$, he cannot send $AC_A$ to $U_B$. Therefore, if the parameter $\tau$ is larger than or equal to the parameter $AT$, there is no duplicate agent in an AC’s EQ. In other words, an AC never reaches an agent twice when $\tau$ is equal to $AT$. In this thesis, we assign $\tau$ to $AT$.

### 4.5.6 AC Timeout

Let $AT$ denote the timeout of ACs. An AC expires $AT$ seconds after it is generated. When an AC expires, all agents delete the AC information from their memory.
4.6 Protocol Details

4.6.1 Generating ACs

Maintaining a certain number of ACs in the network is a prerequisite for users for sending queries. Considering that ACs can expire, users must generate ACs continuously. The user who generates an AC is called the creator of the AC; at the same time, he is also the first agent of the AC. ACs are created based on two principles: fairness and continuity.

ACs impose a burden on agents. In fact, agents are unlikely to benefit from relaying messages to the original requester because they need to allocate memory to save ACs’ information and consume energy to forward replies. To prevent users who generate more ACs than others from being overloaded, some fairness mechanism must be in place to ensure that all users generate a relatively equal number of ACs.

We assume that $AT = 30$ minutes, and every user generates 100 ACs at the beginning and generates no AC until the 30th minute. Since all agents remove the information of expired ACs from their memory, they can hardly deliver replies which use expired ACs. As a result, it is hard for an user to select an appropriate AC for his query at the 29th minute when all ACs only have 1 (= 30 − 29) more minute, because agents may not be able to forward the reply of his query even though the LBS receives the query successfully. Therefore, the generating strategy should be steady and sustainable.

In our protocol, each user generates a new AC every $GP$ second. Since an AC has an $AT$-seconds timeout, there are $\delta = \frac{AT}{GP}$ ACs held by each user in the network. In other words, each user maintains about $\delta$ ACs which is generated by himself, and we meet the fairness criteria. Since users create ACs continuously, ACs have various timeouts so that it is likely for an user to pick an AC which does not expire in a long time (at least longer than his queries and replies).
4.6.2 Exchange Distributing Appointment Cards

Users exchange their *distributing*-ACs as frequently as possible, so that a *distributing*-AC can be switched to a *ready* one quickly. Still, there are some other conditions which should be satisfied when exchanging a *distributing*-AC. Users should avoid giving all their *ready*-ACs to a single user, which leads to identical set of AC agents. As shown in subsection 4.5.4, we use Seg and DLs to separate *distributing*-ACs. We also need to prevent ACs from having duplicate agents using $\tau$ which is described in subsection 4.5.5.

Now we propose the strategy of exchanging *distributing*-ACs. Let us take a pair of users Alice and Bob as an example. If Alice encounters another user Bob, Bob tells Alice whether he trusts her (Bob views her as a friend). Alice picks one of her *distributing*-AC lists (e.g., DL1). Alice traverses all ACs in DL1, and *distributing*-ACs which satisfy the following two conditions should be given to Bob:

1. If the AC’s EQL is not shorter than $k - m$, then Alice must be a friend of Bob.

2. Bob was not carrying the AC in the recent $\tau$ time interval.

When Alice sends a *distributing*-AC to Bob, she adds her identity and the current time to the AC’s EQ. Besides, Alice must modify the AC’s Aid to her own identity and its Aapt to a new random number. She also records the information in Table 4.4 as relay-table in her memory. We should notice that the first agent (i.e., the creator) does not have the Aapt$_{old}$ and the Aid$_{old}$, because he is precisely the one who has generated the AC. In that case the Aapt$_{old}$ and the Aid$_{old}$ indicate the Capt he gives to the AC and his own identity. When Bob gets those ACs, he puts each one of the received *distributing*-ACs in his DLs respectively and randomly. If an AC whose EQL is already equal to $k$, the AC must be switched to a *ready* state when Bob gets it. Bob puts *ready*-ACs in his *ready*-AC list instead of *distributing*-AC lists.
### Table 4.4: Relay Table Entries

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meanings</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Aapt_{old}$</td>
<td>The $Aapt$ generated by the previous agent</td>
</tr>
<tr>
<td>$Aid_{old}$</td>
<td>The identity of the previous agent</td>
</tr>
<tr>
<td>$Aapt_{new}$</td>
<td>The new $Aapt$ (generated by himself)</td>
</tr>
<tr>
<td>$ID_{nxt}$</td>
<td>The identity of the next agent</td>
</tr>
<tr>
<td>$EQL$</td>
<td>The AC’s $EQL$ (should larger than 0)</td>
</tr>
<tr>
<td>$AT$</td>
<td>The time when the AC times out.</td>
</tr>
</tbody>
</table>

### 4.6.3 Exchange Ready Appointment Cards

Users ask for *ready*-ACs only from their friends, which prevents strangers from learning the information of the users who are holding the *ready*-ACs. The strategy of exchanging *ready*-ACs should also meet some fairness criteria. That is, the number of each user’s *ready*-ACs should be more or less equal.

Let us consider two friends Alice and Bob as an example. Alice has 20 ACs, while Bob has 10 ACs. When they encounter each other, it is reasonable that they both give half of their *ready*-ACs to each other. As a result, they both will have half of the total ($\frac{20+10}{2}$) ACs. However, that strategy does not work in the following condition. Alice is a friend of Bob, while Bob is not a friend of Alice. In other words, Bob trusts Alice, but Alice does not trust Bob. We assume that Alice is a trusted but suspicious girl so that many users trust her while she trusts few users while Bob is opposite. When users encounter Alice, they ask for *ready*-ACs from her, but Alice rarely asks for *ready*-ACs. Therefore, Alice carries few *ready*-ACs, while Bob carries many *ready*-ACs. When Alice and Bob encounter each other, and Bob asks for *ready*-ACs, then the strategy seems unfair for Alice. To ensure the fairness and the efficiency of the strategy, users must compare the number of their own *ready*-ACs and the number of *ready*-ACs carried by the other user when two users are exchanging *ready*-ACs.

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When Bob encounters Alice, Bob tells Alice the number of his ready-ACs \(NR_{Bob}\) and whether he wants Alice’s ready-ACs (if he trusts Alice). If Alice learns that Bob needs her ready-ACs, she compares the number of her ready-ACs \(NR_{Alice}\) and \(NR_{Bob}\). If \(NR_{Bob} \geq NR_{Alice}\), Alice gives no ready-AC to Bob; otherwise, she gives \(\frac{NR_{Alice} - NR_{Bob}}{2}\) to Bob. In this way, ready-ACs do not concentrate in a group of users who trust many users.

The process of exchanging ready-ACs is much more straightforward than that for distributing-ACs. Users do not modify any information in the ready-ACs including \(Aapt\) and \(Aid\) so that the parameters of ready-ACs always stay the same.

The algorithm of exchanging ACs when an user \(U_i\) encounters another user \(U_j\) is shown in Algorithm 4.1. The two users tell each other whether they are friends at the very beginning of their encounter. After they both know their relationship, they start to exchange their distributing-ACs. When they both finish receiving the distributing-ACs from the other, they continue to exchange their ready-ACs at the same time. The process ends when they finish exchanging their ready-ACs (or they do not need to exchange ready-ACs).

### 4.6.4 Sending Queries

The original requester must be able to send his queries to the LBSP and be able to get the reply while preventing the LBSP from learning his identity. In ACP, the original requester sends his query using \(Agt_1\)’s identity to the LBSP, and \(Agt_1\) is responsible for forwarding the reply from LBSP to the original requester. Therefore, the original requester’s query includes a sender identity \(Agt_1\), which is equal to the \(Cid\) in the AC. Since \(Agt_1\) needs a \(Capt\) to identify the AC used by the query (and the reply), the \(Capt\) in the AC is also in the query. The network can deliver that query to the destination LBSP efficiently with any DTN protocol.

We use the example in Figure 4.1. The original requester \(U_d\) has an AC (i.e., \(AC_{a,c}^{\beta}\)) whose creator is \(U_a\). When \(U_d\) uses \(AC_{a,c}^{\beta}\) to send his query \(Query_{d}^{a(\beta)}\), the sender identity
Algorithm 4.1 Algorithm for exchanging ACs

1: procedure Encounte$(U_j)$
2:     if $U_i$ trusts $U_j$ then
3:         $U_i$ tells $U_j$ that $U_j$ is viewed as a friend.
4:     else
5:         $U_i$ tells $U_j$ that $U_j$ is not viewed as a friend.
6:     end if
7:     Wait for $U_j$ to tell $U_i$ whether $U_i$ is viewed as a friend.
8:     $U_i$ chooses a distributing list ($DL_\omega$) randomly.
9:     for each $AC_u$ in $DL_\omega$ do
10:        if $U_j$ was carrying $AC_u$ in the recent $\tau$ time then
11:           $AC_u$ cannot be sent to $U_j$
12:           continue (Try the next one.)
13:        end if
14:        if the $EQL$ of $AC_u \geq k - m$ then
15:           if $U_i$ is not trusted by $U_j$ then
16:              $AC_u$ cannot be sent to $U_j$
17:              continue (Try the next one.)
18:           end if
19:        end if
20:        Send $AC_u$ to $U_j$
21:     end for
22:     Tell $U_j$ that all distributing-ACs are sent.
23:     Receive all distributing-ACs from $U_j$
24:     if $U_i$ trusts $U_j$ then
25:         $U_i$ tells $U_j$ $NR_i$.
26:     end if
27:     if $U_i$ is trusted by $U_j$ then
28:        Wait for $U_j$ to tell $U_i$ $NR_j$.
29:        if $NR_j \geq NR_i$ then
30:           send no ready-AC to $U_j$
31:        else
32:           send $\frac{NR_i - NR_j}{2}$ number of ready-ACs to $U_j$
33:        end if
34:     Tell $U_j$ all ready-ACs are sent.
35:     end if
36:     if $U_i$ trusts $U_j$ then
37:        Wait for ready-ACs from $U_j$.
38:     end if
39: end procedure
is $a$, and the $Capt$ of the query is the $capt_\alpha^\beta$, as shown in Figure 4.5.

<table>
<thead>
<tr>
<th>$AC_{a,c}^\beta$</th>
<th>$Query_{d}^{a(\beta)}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cid</td>
<td>$a$</td>
</tr>
<tr>
<td>Capt</td>
<td>$capt_\alpha^\beta$</td>
</tr>
<tr>
<td>Aid</td>
<td>$c$</td>
</tr>
<tr>
<td>Aapt</td>
<td>$aapt_{c}^{a(\beta)}$</td>
</tr>
<tr>
<td>$EQL$</td>
<td>$3$</td>
</tr>
<tr>
<td></td>
<td>$Sender$</td>
</tr>
<tr>
<td></td>
<td>$a$</td>
</tr>
<tr>
<td></td>
<td>$Receiver$</td>
</tr>
<tr>
<td></td>
<td>$LBS$ provider</td>
</tr>
<tr>
<td></td>
<td>$Capt$</td>
</tr>
<tr>
<td></td>
<td>$capt_\alpha^\beta$</td>
</tr>
</tbody>
</table>

Figure 4.5: Constitute Query

The AC is marked as used when the query is ready to be sent so that the AC cannot be given to other users. The original requester also uses a pseudonym to receive the reply, which is described in subsection 4.6.5.4. The algorithm that an user $U_i$ uses to send a query is shown in Algorithm 4.2.

**Algorithm 4.2** Algorithm for Sending Queries

1: **procedure** SendQuery
2: Choose an ready-AC or used-AC, say $AC_{a,f}^\beta$.
3: if The AC is in the ready state then
4: Switch the AC to the used state.
5: end if
6: Assign the sender identity of the query to $U_a$
7: Assign the receiver identity to the LBS
8: Assign the $AN$ to the $capt_\alpha^\beta$
9: Get a pseudonym $pseudo(U_f, aapt_{f}^{a(\beta)})$
10: Use the pseudonym as $U_i$’s identity.
11: Send the query to the LBS.
12: **end procedure**

### 4.6.5 Sending Replies

#### 4.6.5.1 The LBSP part

When the LBSP receives the query, it learns that the sender’s identity is the first agent $U_a$ instead of the original requester $U_d$, which protects the location privacy of the original
requester. In Figure 4.6, the LBS provider replies to the sender $U_a$, when it receives $Query_{d}^{a(\beta)}$. The reply also includes the $Capt$ of the query (i.e., $capt_{a}^{\beta}$), which enables $U_a$ to identify the AC used in the query and the reply.

![Figure 4.6: Constitute Replies](image)

4.6.5.2 The First Agent

When the first agent (i.e., $Agt_1$) gets the reply from the LBSP, he learns the $AN$ in the reply. He searches his reply-table to get the information of the AC used in the query and reply. If the AC does not expire, there must be a corresponding entry in his reply-table. As shown in Table 4.5, it should be an entry where the $Aid_{old}$ and $Aapt_{old}$ are equal to $Agt_1$’s identity and the $AN$ of the reply, respectively. As a result, $Agt_1$ learns the identity of the next agent (i.e., $Agt_2$) from the $ID_{nxt}$ of the entry, so $Agt_1$ forwards the reply to $Agt_2$. The $AN$ of the reply is replaced with the $Aapt_{new}$ in the entry by $Agt_1$, which enables $Agt_2$ to identify the AC in $Agt_2$’s reply-table.

Table 4.5: Reply Table Entries of The First Agent

<table>
<thead>
<tr>
<th>Name of Entries</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Aid_{old}$</td>
<td>The user’s own identity</td>
</tr>
<tr>
<td>$Aapt_{old}$</td>
<td>The $Capt$ of the AC used in the reply (query)</td>
</tr>
<tr>
<td>$ID_{nxt}$</td>
<td>The identity of the second agent</td>
</tr>
<tr>
<td>$Aapt_{new}$</td>
<td>The $Aapt$ given to the second agent by the user.</td>
</tr>
<tr>
<td>$EQL$</td>
<td>1</td>
</tr>
<tr>
<td>$AT$</td>
<td>The time when the AC times out.</td>
</tr>
</tbody>
</table>
For the example in Figure 4.1, the first agent is $U_a$. When he receives $\text{Reply}^{a(\beta)}_{\text{LBS}}$, he learns that it is a reply from the LBS and the $\text{Capt}$ of the AC is $\text{capt}_a^3$. He searches his reply-table for an entry whose $Aid_{old}$ is equal to $a$ and $Aapt_{old}$ is equal to $\text{capt}_a^3$. As shown in Figure 4.7, the $ID_{nxt}$ in the entry is equal to $b$ so he modifies the receiver of the reply message to $U_b$. $U_a$ also modifies the AN in the reply message to $\text{aapt}_a^{a(\beta)}$ which is exactly equal to the $Aapt_{new}$ in his reply-table entry, which enables $U_b$ identifies the AC in his reply-table.

![Reply table entry](image)

Figure 4.7: The Reply of The First Agent

### 4.6.5.3 Intermediate Agents

The process of forwarding replies in the intermediate agents (the second to the $(k - 1)^{th}$ one) is similar to that of the first agent. We take the second agent as an example. When the second agent receives the reply forwarded by the first one, he learns the sender’s identity (i.e., the first agent) and the AN from the reply. In his reply-table shown in Table 4.6, the corresponding entry for the AC used in the reply have $Aid_{old}$ of $Agt_1$ and $Aapt_{old}$ of $Aapt$ given by $Agt_1$, because he gets the AC from the first agent. More specifically, his reply-table must include an entry whose $Aid_{old}$ is equal to the previous agent’s identity and the $Aapt_{old}$ is the value of AN in the received reply.

For the example in Figure 4.1, the second agent is $U_b$. When he receives $\text{Reply}_a^{a(\beta)}$, he learns that it is $U_a$ who forwards the reply message $\text{Reply}_a^{a(\beta)}$ and the $Aapt$ of the AC is $\text{aapt}_a^{a(\beta)}$. He searches his reply-table for an entry whose $Aid_{old}$ is equal to $a$ and $Aapt_{old}$
Table 4.6: Reply Table Entries of The Second Agent

<table>
<thead>
<tr>
<th>Name of Entries</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aid\textsubscript{old}</td>
<td>The identity of the previous agent (i.e. the first agent)</td>
</tr>
<tr>
<td>Aapt\textsubscript{old}</td>
<td>The Aapt given by the previous agent.</td>
</tr>
<tr>
<td>ID\textsubscript{nxt}</td>
<td>The identity of the next agent (e.g. the third agent)</td>
</tr>
<tr>
<td>Aapt\textsubscript{new}</td>
<td>The Aapt given to the next agent by the user.</td>
</tr>
<tr>
<td>EQL</td>
<td>2</td>
</tr>
<tr>
<td>AT</td>
<td>The time when the AC times out.</td>
</tr>
</tbody>
</table>

is equal to $a\text{apt}\textsubscript{a(β)}$. As shown in Figure 4.8, since the ID\textsubscript{nxt} in the entry is equal to $c$, he modifies the receiver of the reply message to $U_c$. $U_b$ also modifies the AN in the reply message to $a\text{apt}\textsubscript{b(β)}$ which enables $U_c$ identifies the AC in $U_c$’s reply-table, because the $Aapt\textsubscript{new}$ in the entry is equal to $a\text{apt}\textsubscript{b(β)}$.

![Reply table entry](image)

Figure 4.8: The Reply of The Second Agent

For each agent $Agt_i$, where $2 \leq i \leq k - 1$, he searches his reply-table for the corresponding entry when he receives a reply. The Aid\textsubscript{old} and Aapt\textsubscript{old} in the entry should be equal to the sender’s identity and the AN in the reply. The identity of the next agent $Agt_{i+1}$ is ID\textsubscript{nxt}. $Agt_i$ also assigns Aapt\textsubscript{new} to the AN in the reply to help $Agt_{i+1}$ search $Agt_{i+1}$’s reply-table.
### 4.6.5.4 The Last Agent

The last agent also searches for a *reply-table* entry based on the reply, while he cannot get the identity of the next agent. The *reply-table* entry of the last agent is shown in Table 4.7.

<table>
<thead>
<tr>
<th>Name of Entries</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Aid_{old}$</td>
<td>The identity of the previous agent (i.e., the second agent)</td>
</tr>
<tr>
<td>$Aapt_{old}$</td>
<td>The $Aapt$ given by the previous agent.</td>
</tr>
<tr>
<td>$ID_{nxt}$</td>
<td>VOID</td>
</tr>
<tr>
<td>$Aapt_{new}$</td>
<td>The $Aapt$ given to the original requester.</td>
</tr>
<tr>
<td>$EQL$</td>
<td>$k$</td>
</tr>
<tr>
<td>$AT$</td>
<td>The time when the AC times out.</td>
</tr>
</tbody>
</table>

The last agent uses the same way to look the entry up in his *reply-table* based on the reply. When he finds that the $EQL$ is equal to $k$, he notices that he is the last agent. Then, he is responsible for forwarding the reply to the original requester instead of forwarding to another agent. He uses his identity and $Aapt_{new}$ in his *reply-table* entry to generates a pseudonym as follows:

$$psd^{a(\beta)}_{Agt_k} = pseudo(Agt_k, Aapt_{new}) \quad (4.1)$$

where the function $pseudo(id, Aapt)$ is a public pseudonym generating function which everyone in the network knows, including the original requester.

When the original requester sends his query, he also gets the same pseudonym $psd^{a(\beta)}_{Agt_k}$ using the pseudonym generating function. Note that he can get parameters from the AC. $Agt_k$ and $Aapt_{new}$ are equal to the $Aid$ and $Aapt$ in the AC. He uses that pseudonym as his identity before he gets the reply.
When users deliver the reply from the last agent, they are looking for an user whose identity is that pseudonym. At last, the original requester gets the reply, because he is the only user who uses the pseudonym as his identity.

For the example in Figure 4.1, the last agent is $U_c$. When he receives $\text{Reply}^a_{b(\beta)}$, he learns that it is $U_b$ who forwards the reply message $\text{Reply}^a_{b(\beta)}$ and the $Aapt$ of the AC is $aapt^a_{b(\beta)}$. He searches his $\text{reply-table}$ for an entry whose $Aid_{old}$ is equal to $b$ and $Aapt_{old}$ is equal to $aapt^a_{b(\beta)}$. Since the $EQL$ in the entry is equal to 3 (i.e. $k$), he recognizes that he is the last agent. $U_c$ calculates the pseudonym $psd_c^{a(\beta)} = \text{pseudo} \left( c, aapt^a_{c(\beta)} \right)$ then forward the reply to $psd_c^{a(\beta)}$. The original requester $U_d$ gets the identity $c$ and the $aapt^a_{c(\beta)}$ from the AC he uses, so that he uses the pseudonym $psd_c^{a(\beta)}$ as his identity. As a result, $U_d$ get the reply from $U_c$. The $AN$ of the reply is also assigned to $aapt^a_{c(\beta)}$ to avoid identical pseudonyms. The process is shown in Figure 4.9.

![Figure 4.9: The Reply of the Last Agent](image)

The algorithm of forwarding replies when an agent $U_i$ gets a reply message from $U_{prev}$ is shown in Algorithm 4.3. $U_i$ learns the $AN$ and the identity of the sender from the reply message $\text{Reply}^{a(\beta)}_{U_{prev}}$. Based on this information, $U_i$ checks his $\text{reply-table}$ to find out where the reply should be forwarded to, which is $ID_{nxt}$. After $U_i$ updates the $AN$ of the reply message, he forwards the reply message to $ID_{nxt}$.
Algorithm 4.3 Algorithm For Forwarding Replies

1: procedure RECEIVED(Reply$^αβ_{U_{prev}}$)
2:     Get the AN from Reply$^αβ_{U_{prev}}$
3:     if $U_{prev}$ is the LBS then
4:         search $U_i$’s relay-table to find an entry $E_α^β_{i}^{old}$
5:             whose $Aapt_{old} = AN$ and $Aid_{old} = U_i$
6:     else
7:         search $U_i$’s relay-table to find an entry $E_α^β_{i}^{old}$
8:             whose $Aapt_{old} = AN$ and $Aid_{old} = U_{prev}$
9:     end if
10:     Get the EQL, $Aapt_{new}$ and $ID_{nxt}$ from $E_α^β_{i}$
11:     Assign the AN of Reply$^αβ_{U_{prev}}$ to $Aapt_{new}$.
12:     Assign the sender identity to $U_i$.
13:     if $EQL = k$ then
14:         $ID_{nxt} ←$ pseudo($U_i, Aapt_{new}$)
15:     end if
16:     Forward the reply to $ID_{nxt}$
17: end procedure

4.7 Appointment Number

The Appointment Number (AN) including Capt and Aapt is significant information in the AC. We explain the rules of generating them in detail and talk about the effect of ACs’ timeout mechanism in this section.

4.7.1 Creator Appointment Number

The Creator Appointment Number (Capt) is a number which is used to identify ACs generated by the same creator. In other words, if two ACs are generated by the same creator, and they do not expire, their Capt must be different. Therefore, the first agent (i.e., the creator) cannot find two entries which have the same $Aapt_{old}$ in his reply-table, if their $Aid_{old}$ are both his own identity.
4.7.2 Agent Appointment Number

The Agent appointment number ($Aapt$) is a number used to identify ACs which have the same agent. Agents generate a new $Aapts$ for ACs before they exchange those cards to others. In other words, an agent gives any AC passing on by him a unique $Aapt$, which helps the next agent identify the AC in his reply-table. Since the $Aapt$ is unique, an agent who is not the first one cannot find the replicated pair, $Aid_{old}$ and $Aapt_{old}$, in his reply-table.

4.7.3 Timeout

Agents delete the entries, which contains the information of expired ACs, from his reply-table. Consequently, agents cannot forward replies using ACs which expire. That is the reason why an original requester must choose an AC which expires after his query and reply time out. However, the timeout mechanism is still necessary for the protocol.

Since users are moving, the distance between agents and the original requester might be too large after a long time. As a result, it is hard for agents to forward the reply messages back to the original requester so that the original requester takes a high risk when he uses an AC which exists for a long time. Then this kind of ACs might not be used after a period, while it cost agents a few memories to save the ACs’ information in their reply-table. Therefore, all users remove the information of expired ACs to save their memories.

We should also notice that an unexpired AC and an expired one might have the same $Capt$ or $Aapt$. Because no agent keeps the record of the expired AC, the duplication cannot confuse agents.
4.8 Example

In the following example, we use 5 users (i.e., Alice, Bob, Charlie, David and Elizabeth) to show the process of ACP. We should notice that David trusts Charlie (Charlie does not trust David), Elizabeth trusts David (David does not trust Elizabeth). Users do not trust others except the above two pairs. The parameters are shown in Table 4.8.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k$</td>
<td>3</td>
</tr>
<tr>
<td>$m$</td>
<td>1</td>
</tr>
<tr>
<td>$Seg$</td>
<td>2</td>
</tr>
<tr>
<td>$GP$</td>
<td>10 minutes</td>
</tr>
<tr>
<td>$AT$</td>
<td>80 minutes</td>
</tr>
<tr>
<td>$\tau$</td>
<td>80 minutes (equal to $AT$)</td>
</tr>
</tbody>
</table>

We abstract the event that users encounter each other in Table 4.9. Let $t_i$ denote the $i^{th}$ minute. The table lists the time when two users encounter each other. For example, Charlie and Elizabeth encounter each other at the third minute ($t_3$). After two users meet, they separate in one minute.

We assume that these users do not encounter any user for a long time, so that they each has $8\left(=\frac{80\text{min}}{10\text{min}}\right)$ ACs generated by themselves. We also assume that no AC expires in our 8-minutes example. Since the parameter $Seg$ is equal to 2, each user has 2 Distributing AC Lists ($DL$s). The initial state of our example is shown in Table 4.10. To make the example simple and clear, we do not place ACs in $DL$s randomly, ACs are always placed in the DL alternately. For example, if we put the first AC in $DL_1$, then the second AC must be in the $DL_2$. Users also obey the rule when they receive ACs from other users.

The explanation of symbols used in table are shown in the former Table 4.1. To make the symbol clear, we add the $EQL$ of the AC on the superscript. For example, if the $EQL$
Table 4.9: Example Event

<table>
<thead>
<tr>
<th>User 1</th>
<th>User 2</th>
<th>Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elizabeth</td>
<td>Bob</td>
<td>$t_1$</td>
</tr>
<tr>
<td>Bob</td>
<td>Charlie</td>
<td>$t_2$</td>
</tr>
<tr>
<td>Charlie</td>
<td>Elizabeth</td>
<td>$t_3$</td>
</tr>
<tr>
<td>Elizabeth</td>
<td>Alice</td>
<td>$t_4$</td>
</tr>
<tr>
<td>Bob</td>
<td>Charlie</td>
<td>$t_5$</td>
</tr>
<tr>
<td>Alice</td>
<td>Charlie</td>
<td>$t_6$</td>
</tr>
<tr>
<td>Charlie</td>
<td>David</td>
<td>$t_7$</td>
</tr>
<tr>
<td>David</td>
<td>Elizabeth</td>
<td>$t_8$</td>
</tr>
</tbody>
</table>

Table 4.10: Example Initial State

<table>
<thead>
<tr>
<th>User Identity</th>
<th>$DL1$</th>
<th>$DL2$</th>
<th>$RL$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alice (A)</td>
<td>$AC_A^{1[0]}$, $AC_A^{3[0]}$, $AC_A^{5[0]}$, $AC_A^{7[0]}$</td>
<td>$AC_A^{2[0]}$, $AC_A^{4[0]}$, $AC_A^{6[0]}$, $AC_A^{8[0]}$</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>Bob (B)</td>
<td>$AC_B^{1[0]}$, $AC_B^{3[0]}$, $AC_B^{5[0]}$, $AC_B^{7[0]}$</td>
<td>$AC_B^{2[0]}$, $AC_B^{4[0]}$, $AC_B^{6[0]}$, $AC_B^{8[0]}$</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>Charlie (C)</td>
<td>$AC_C^{1[0]}$, $AC_C^{3[0]}$, $AC_C^{5[0]}$, $AC_C^{7[0]}$</td>
<td>$AC_C^{2[0]}$, $AC_C^{4[0]}$, $AC_C^{6[0]}$, $AC_C^{8[0]}$</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>David (D)</td>
<td>$AC_D^{1[0]}$, $AC_D^{3[0]}$, $AC_D^{5[0]}$, $AC_D^{7[0]}$</td>
<td>$AC_D^{2[0]}$, $AC_D^{4[0]}$, $AC_D^{6[0]}$, $AC_D^{8[0]}$</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>Elizabeth (E)</td>
<td>$AC_E^{1[0]}$, $AC_E^{3[0]}$, $AC_E^{5[0]}$, $AC_E^{7[0]}$</td>
<td>$AC_E^{2[0]}$, $AC_E^{4[0]}$, $AC_E^{6[0]}$, $AC_E^{8[0]}$</td>
<td>$\emptyset$</td>
</tr>
</tbody>
</table>
of $AC^{1}_{A,X}$ is equal to 2, it is marked as $AC^{1[2]}_{A,X}$.

### 4.8.1 Exchanging Appointment Cards

To make it easier, users do not pick DLs randomly as we described in the previous sections when they exchange ACs. Instead, if we say that $U_x$ encounters $U_y$, $U_x$ always picks his DL1 and $U_y$ always picks his DL2.

The tables in current section show the entire distributing-AC Lists (i.e., DL1 and DL2) and entire relay-tables (RLs) of each user. We use the initial letter to denote each user in symbols. For example, D denotes David. The structure of the AC-list tables is shown in Table 4.11.

<table>
<thead>
<tr>
<th></th>
<th>X</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>DL1</td>
<td>Before X’s distributing-AC list 1 before their exchange.</td>
<td>Before Y’s distributing-AC list 1 before their exchange.</td>
</tr>
<tr>
<td></td>
<td>After X’s distributing-AC list 1 after their exchange.</td>
<td>After Y’s distributing-AC list 1 after their exchange.</td>
</tr>
<tr>
<td>DL2</td>
<td>Before X’s distributing-AC list 2 before their exchange.</td>
<td>Before Y’s distributing-AC list 2 before their exchange.</td>
</tr>
<tr>
<td></td>
<td>After X’s distributing-AC list 2 after their exchange.</td>
<td>After Y’s distributing-AC list 2 after their exchange.</td>
</tr>
<tr>
<td>RL</td>
<td>Before X’s ready-AC list before their exchange.</td>
<td>Before Y’s ready-AC list before their exchange.</td>
</tr>
<tr>
<td></td>
<td>After X’s ready-AC list after their exchange.</td>
<td>After Y’s ready-AC list after their exchange.</td>
</tr>
</tbody>
</table>

The process of exchanging AC is shown step by step as follows.

1. Elizabeth encounters Bob
At $t_1$ (the first minute), Elizabeth encounters Bob. Elizabeth picks her $DL_1$, and Bob picks his $DL_2$. They give distributing-ACs in their picked $DL$s to each other and update their reply tables, as shown in Table 4.12 and Table 4.13.

### Table 4.12: Elizabeth and Bob’s AC Lists at Time $t_1$

<table>
<thead>
<tr>
<th></th>
<th>$DL_1$</th>
<th>Before</th>
<th>$AC_1^{[0]}_E, AC_3^{[0]}_E, AC_5^{[0]}_E, AC_7^{[0]}_E$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>After</td>
<td>$AC_2^{[1]}<em>{B,B}, AC_6^{[1]}</em>{B,B}$</td>
<td></td>
</tr>
<tr>
<td>$DL_2$</td>
<td>Before</td>
<td>$AC_2^{[0]}_E, AC_4^{[0]}_E, AC_6^{[0]}_E, AC_8^{[0]}_E$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>After</td>
<td>$AC_2^{[0]}_E, AC_4^{[0]}_E, AC_6^{[0]}<em>E, AC_8^{[0]}<em>E, AC_4^{[1]}</em>{B,B}, AC_8^{[1]}</em>{B,B}$</td>
<td></td>
</tr>
<tr>
<td>$RL$</td>
<td>Before</td>
<td>$\emptyset$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>After</td>
<td>$\emptyset$</td>
<td></td>
</tr>
</tbody>
</table>

### Table 4.13: Elizabeth and Bob’s Relay Table At Time $t_1$

<table>
<thead>
<tr>
<th></th>
<th>$Aid_{old}$</th>
<th>$Aapt_{old}$</th>
<th>$ID_{nxt}$</th>
<th>$Aapt_{new}$</th>
<th>$EQL$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elizabeth</td>
<td>$E$</td>
<td>$capt_1^E$</td>
<td>$B$</td>
<td>$aapt_1^E$</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>$E$</td>
<td>$capt_3^E$</td>
<td>$B$</td>
<td>$aapt_3^E$</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>$E$</td>
<td>$capt_5^E$</td>
<td>$B$</td>
<td>$aapt_5^E$</td>
<td>1</td>
</tr>
<tr>
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<td>$aapt_8^B$</td>
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</tbody>
</table>

2. Bob encounters Charlie

At $t_2$ (the second minute), Bob encounters Charlie. Bob picks his $DL_1$, and Charlie picks his $DL_2$. They give distributing-ACs in their picked $DL$s to each other and update their reply tables, as shown in Table 4.14 and Table 4.15.
Table 4.14: Bob and Charlie’s AC Lists at Time $t_2$

|       | Bob          |               |               |               |               |               |               | Charlie       |               |               |               |               |               |               |               |               |
|-------|--------------|---------------|---------------|---------------|---------------|---------------|---------------|--------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
|       | DL1          | Before $AC_{B,DL1}^{1[0]}$, $AC_{B,DL1}^{2[0]}$, $AC_{B,DL1}^{4[0]}$, $AC_{B,DL1}^{7[0]}$, $AC_{E,DL1}^{1[1]}$, $AC_{E,DL1}^{5[1]}$ | After $AC_{C,DL2}^{2[1]}$, $AC_{C,DL2}^{6[1]}$ |               |               |               |               | DL2          | Before $AC_{C,DL2}^{3[1]}$, $AC_{C,DL2}^{7[1]}$ | After $AC_{E,DL1}^{3[1]}$, $AC_{E,DL1}^{4[1]}$, $AC_{C,DL2}^{8[1]}$ |               |               |               |               |
|       | DL2          | Before $AC_{E,DL2}^{3[1]}$, $AC_{E,DL2}^{7[1]}$ | After $AC_{E,DL2}^{3[1]}$, $AC_{C,DL2}^{8[1]}$ |               |               |               |               | RL           | Before $\emptyset$ | After $\emptyset$ |               |               |               |               |
|       | RL           | Before $\emptyset$ | After $\emptyset$ |               |               |               |               |              |               |               |               |               |               |               |               |

Table 4.15: Bob and Charlie’s Relay Table At Time $t_2$

|       | Bob |               |               |               |               |               |               | Charlie |               |               |               |               |               |               |               |               |
|-------|-----|---------------|---------------|---------------|---------------|---------------|---------------|---------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
|       | Aid$_{old}$ | $Aapt_{old}$ | $ID_{nxt}$ | $Aapt_{new}$ | EQL | Aid$_{old}$ | $Aapt_{old}$ | $ID_{nxt}$ | $Aapt_{new}$ | EQL |
|       | B   | $capt_{B}^{2}$ | $E$ | $aapt_{B}^{2(2)}$ | 1 | C | $capt_{C}^{2}$ | B | $aapt_{C}^{2(2)}$ | 1 |
|       | B   | $capt_{B}^{4}$ | $E$ | $aapt_{B}^{2(4)}$ | 1 | C | $capt_{C}^{4}$ | B | $aapt_{C}^{2(4)}$ | 1 |
|       | B   | $capt_{B}^{6}$ | $E$ | $aapt_{B}^{2(6)}$ | 1 | C | $capt_{C}^{6}$ | B | $aapt_{C}^{2(6)}$ | 1 |
|       | B   | $capt_{B}^{8}$ | $E$ | $aapt_{B}^{2(8)}$ | 1 | C | $capt_{C}^{8}$ | B | $aapt_{C}^{2(8)}$ | 1 |
|       | B   | $capt_{B}^{1}$ | $C$ | $aapt_{B}^{2(1)}$ | 1 |               |               |               |               |               |               |               |               |               |               |               |
|       | B   | $capt_{B}^{3}$ | $C$ | $aapt_{B}^{2(3)}$ | 1 |               |               |               |               |               |               |               |               |               |               |               |
|       | B   | $capt_{B}^{5}$ | $C$ | $aapt_{B}^{2(5)}$ | 1 |               |               |               |               |               |               |               |               |               |               |               |
|       | B   | $capt_{B}^{7}$ | $C$ | $aapt_{B}^{2(7)}$ | 1 |               |               |               |               |               |               |               |               |               |               |               |
|       | E   | $aapt_{E}^{1(1)}$ | $C$ | $aapt_{B}^{2(1)}$ | 2 |               |               |               |               |               |               |               |               |               |               |               |
|       | E   | $aapt_{E}^{1(5)}$ | $C$ | $aapt_{B}^{2(5)}$ | 2 |               |               |               |               |               |               |               |               |               |               |               |

3. Charlie encounters Elizabeth

At time $t_3$, Charlie encounters Elizabeth. Charlie picks his $DL1$, and Elizabeth picks her $DL2$. They give *distributing*-ACs in their picked $DL$s to each other and update their
reply tables, as shown in Table 4.16 and Table 4.17.

We should notice that Charlie does not give $AC_{E,B}^{1[2]}$ to Elizabeth, because Elizabeth does not trust Charlie. The EQL of the $AC_{E,B}^{1[2]}$ has already reached 2, which is equal to $k - m = 3 - 1$. As mentioned in subsection 4.6.2, these kinds of ACs are only sent to users who trust the current agent. Therefore, Charlie cannot give $AC_{E,B}^{1[2]}$ to Elizabeth when she does not trust him.

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<th>Table 4.16: Charlie and Elizabeth’s AC Lists at Time $t_3$</th>
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<tr>
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<td><strong>DL2</strong> Before</td>
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<td>After</td>
</tr>
<tr>
<td><strong>RL</strong> Before</td>
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</tbody>
</table>

| **Elizabeth** |
| **DL1** Before | $AC_{B,B}^{2[1]}, AC_{B,B}^{6[1]}$ |
| After | $AC_{B,B}^{2[1]}, AC_{B,B}^{6[1]}, AC_{C,C}^{1[1]}, AC_{C,C}^{5[1]}, AC_{B,C}^{1[2]}$ |
| **DL2** Before | $AC_{E}^{2[0]}, AC_{E}^{4[0]}, AC_{E}^{6[0]}, AC_{E}^{8[0]}, AC_{B,B}^{4[1]}, AC_{B,B}^{8[1]}$ |
| After | $AC_{C,C}^{3[1]}, AC_{C,C}^{7[1]}, AC_{B,C}^{5[2]}$ |
| **RL** Before | $\emptyset$ |
| After | $\emptyset$ |
4. Elizabeth encounters Alice

At time $t_4$, Elizabeth encounters Alice. Elizabeth picks her $DL_1$, and Alice picks her $DL_2$. They give distributing-ACs in their picked $DLs$ to each other and update their reply tables, as shown in Table 4.18 and Table 4.19.

Elizabeth does not give $AC_{1[2]}^{B,C}$ to Alice for the same reason as the previous Charlie, that is, Alice does not trust Elizabeth.
### Table 4.18: Elizabeth and Alice’s AC Lists at Time $t_4$

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<th>DL2 Before</th>
<th>DL2 After</th>
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<td>$AC_{B,C}^{1[2]} \cdot AC_{A,A}^{2[1]} \cdot AC_{A,A}^{6[1]}$</td>
<td>$AC_{C,C}^{3[1]} \cdot AC_{C,C}^{7[1]} \cdot AC_{B,C}^{5[2]}$</td>
<td>$AC_{C,C}^{3[1]} \cdot AC_{C,C}^{7[1]} \cdot AC_{B,C}^{5[2]} \cdot AC_{B,A}^{4[1]} \cdot AC_{A,A}^{8[1]}$</td>
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<tr>
<td>Alice</td>
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<td>$AC_{A}^{1[0]} \cdot AC_{A}^{3[0]} \cdot AC_{A}^{5[0]} \cdot AC_{A}^{7[0]} \cdot AC_{B,E}^{2[2]} \cdot AC_{C,E}^{1[2]}$</td>
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### Table 4.19: Elizabeth and Alice’s Relay Table At Time $t_4$

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5. Bob encounters Charlie

At time $t_5$, Bob encounters Charlie. Bob picks his DL1, and Charlie picks his DL2. They give distributing-ACs in their picked DLs to each other and update their reply tables, as shown in Table 4.20 and Table 4.21.

Charlie does not give $AC^{5[2]}_{E,B}$ and $AC^{8[2]}_{B,E}$ to Bob, because Bob does not trust Charlie. Since we set the avoiding time equal to $AT$, a distributing-AC cannot be given back to previous agents. As a result, $AC^{2[1]}_{C,C}$, $AC^{6[1]}_{C,C}$, $AC^{3[1]}_{B,B}$ and $AC^{7[1]}_{B,B}$ are not exchanged by Charlie and Bob.

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<tr>
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<td>$AC^{5[1]}<em>{E,E} AC^{7[1]}</em>{E,E} AC^{4[1]}<em>{C,C} AC^{8[1]}</em>{C,C}$</td>
<td>$AC^{5[1]}<em>{E,E} AC^{7[1]}</em>{E,E} AC^{4[1]}<em>{C,C} AC^{8[1]}</em>{C,C} AC^{8[2]}_{E,C}$</td>
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<tr>
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Table 4.20: Bob and Charlie’s AC Lists at Time $t_5$
Table 4.21: Bob and Charlie’s Relay Table At Time $t_5$

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<td>aapt&lt;sup&gt;E(5)&lt;/sup&gt;&lt;sub&gt;B&lt;/sub&gt;</td>
<td>2</td>
<td>$B$</td>
<td>aapt&lt;sup&gt;B(5)&lt;/sup&gt;&lt;sub&gt;B&lt;/sub&gt;</td>
<td>$E$</td>
<td>aapt&lt;sup&gt;B(5)&lt;/sup&gt;&lt;sub&gt;C&lt;/sub&gt;</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$E$</td>
<td>aapt&lt;sup&gt;E(4)&lt;/sup&gt;&lt;sub&gt;E&lt;/sub&gt;</td>
<td>$B$</td>
<td>aapt&lt;sup&gt;E(4)&lt;/sup&gt;&lt;sub&gt;C&lt;/sub&gt;</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>$E$</td>
<td>aapt&lt;sup&gt;E(8)&lt;/sup&gt;&lt;sub&gt;E&lt;/sub&gt;</td>
<td>$B$</td>
<td>aapt&lt;sup&gt;E(8)&lt;/sup&gt;&lt;sub&gt;C&lt;/sub&gt;</td>
<td>2</td>
</tr>
</tbody>
</table>

6. Alice encounters Charlie

At time $t_6$, Alice encounters Charlie. Alice picks her $DL1$, and Charlie picks his $DL2$. They give *distributing*-ACs in their picked $DLs$ to each other and update their reply tables, as shown in Table 4.22 and Table 4.23.
Table 4.22: Alice and Charlie’s AC Lists at Time $t_6$

|        | $DL1$       | Before | $AC_1^{[0]}, AC_3^{[0]}, AC_5^{[0]}, AC_7^{[0]}, AC_2^{[2]}_B,E, AC_1^{[1]}_C,E$ |
|        |             | After  | $AC_2^{[2]}_B,E, AC_1^{[2]}_C,E, AC_3^{[2]}_B,C$ |
|        | $DL2$       | Before | $AC_6^{[2]}_B,E, AC_5^{[2]}_C,E$ |
|        |             | After  | $AC_6^{[2]}_B,E, AC_5^{[2]}_C,E, AC_7^{[2]}_B,C$ |
|        | $RL$        | Before | $\emptyset$ |
|        |             | After  | $\emptyset$ |

|        | $DL1$       | Before | $AC_1^{[2]}_E,B, AC_2^{[1]}_E,E, AC_6^{[1]}_E,E, AC_4^{[2]}_B,E$ |
|        |             | After  | $AC_1^{[2]}_E,B, AC_2^{[1]}_E,E, AC_6^{[1]}_E,E, AC_4^{[2]}_B,E, AC_1^{[1]}_A,A, AC_5^{[1]}_A$ |
|        | $DL2$       | Before | $AC_2^{[1]}_B,B, AC_7^{[1]}_B,B, AC_5^{[2]}_E,B, AC_8^{[2]}_B,E$ |
|        |             | After  | $AC_5^{[2]}_E,B, AC_8^{[2]}_E,B, AC_3^{[1]}_A,A, AC_7^{[1]}_A$ |
|        | $RL$        | Before | $\emptyset$ |
|        |             | After  | $\emptyset$ |

Table 4.23: Alice and Charlie’s Relay Table At Time $t_6$

<table>
<thead>
<tr>
<th></th>
<th>Alice</th>
<th>Charlie</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Aid_{old}$</td>
<td>$Aapt_{old}$</td>
<td>$ID_{nxt}$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_2^A$</td>
<td>$E$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_4^A$</td>
<td>$E$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_6^A$</td>
<td>$E$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_8^A$</td>
<td>$E$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_1^A$</td>
<td>$C$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_3^A$</td>
<td>$C$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_5^A$</td>
<td>$C$</td>
</tr>
<tr>
<td>$A$</td>
<td>$capt_7^A$</td>
<td>$C$</td>
</tr>
</tbody>
</table>

|        | $B$    | $aapt_2^B$  | $E$        | $aapt_2^B$  | 1      |
|        | $B$    | $aapt_5^B$  | $E$        | $aapt_5^B$  | 2      |
|        | $E$    | $aapt_2^E$  | $B$        | $aapt_2^E$  | 2      |
|        | $E$    | $aapt_5^E$  | $B$        | $aapt_5^E$  | 2      |
|        | $B$    | $aapt_2^B$  | $A$        | $aapt_2^B$  | 2      |
|        | $B$    | $aapt_5^B$  | $A$        | $aapt_5^B$  | 2      |
Since Alice and Charlie do not trust each other, $AC_{B,E}^{2[2]}$, $AC_{C,E}^{1[2]}$, $AC_{E,B}^{5[2]}$ and $AC_{B,E}^{8[2]}$ are not exchanged by the two users.

7. Charlie encounters David

At time $t_7$, Charlie encounters David. Charlie pick his $DL_1$, and David picks his $DL_2$. They give distributing-ACs in their picked DLs to each other and update their reply tables, as shown in Table 4.24 and Table 4.25.

Because David trust Charlie, Charlie can give $AC_{E,B}^{1[2]}$ and $AC_{B,E}^{4[2]}$ to David. When David receives $AC_{E,C}^{1[3]}$ and $AC_{B,C}^{4[3]}$, he notices that the EQLs of the two ACs reach $k$ so that he puts these two ACs in his ready list instead of distributing lists.

<table>
<thead>
<tr>
<th></th>
<th>DL1 Before</th>
<th>DL1 After</th>
<th>DL2 Before</th>
<th>DL2 After</th>
<th>RL Before</th>
<th>RL After</th>
</tr>
</thead>
<tbody>
<tr>
<td>Charlie</td>
<td>$AC_{E,B}^{1[2]}, AC_{E,E}^{2[1]}, AC_{E,E}^{6[1]}, AC_{B,E}^{4[2]}, AC_{A,A}^{1[1]}, AC_{A,A}^{6[1]}$</td>
<td>$AC_{B,D}^{2[1]}, AC_{D,D}^{6[1]}$</td>
<td>$AC_{E,B}^{5[2]}, AC_{B,E}^{8[2]}, AC_{A,A}^{3[1]}, AC_{A,A}^{7[1]}$</td>
<td>$AC_{E,B}^{5[2]}, AC_{B,E}^{8[2]}, AC_{A,A}^{3[1]}, AC_{A,A}^{7[1]}, AC_{D,D}^{4[1]}, AC_{D,D}^{8[1]}$</td>
<td>$\emptyset$</td>
<td>$\emptyset$</td>
</tr>
<tr>
<td>David</td>
<td>$AC_{D}^{1[0]}, AC_{D}^{3[0]}, AC_{D}^{5[0]}, AC_{D}^{7[0]}$</td>
<td>$AC_{D}^{2[0]}, AC_{D}^{3[0]}, AC_{D}^{5[0]}, AC_{D}^{7[0]}, AC_{E,C}^{2[2]}, AC_{A,C}^{1[2]}$</td>
<td>$AC_{D}^{2[0]}, AC_{D}^{4[0]}, AC_{D}^{6[0]}, AC_{D}^{8[0]}$</td>
<td>$AC_{D}^{2[0]}, AC_{D}^{4[0]}, AC_{D}^{6[0]}$</td>
<td>$AC_{E,C}^{1[3]}, AC_{A,C}^{4[3]}$</td>
<td>$AC_{E,C}^{1[3]}, AC_{A,C}^{4[3]}$</td>
</tr>
</tbody>
</table>
Table 4.25: Charlie and David’s Relay Table At Time $t_7$

<table>
<thead>
<tr>
<th>$Aid_{old}$</th>
<th>$Aapt_{old}$</th>
<th>$ID_{nxt}$</th>
<th>$Aapt_{new}$</th>
<th>$EQL$</th>
<th>$Aid_{old}$</th>
<th>$Aapt_{old}$</th>
<th>$ID_{nxt}$</th>
<th>$Aapt_{new}$</th>
<th>$EQL$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C$</td>
<td>$capt^2_C$</td>
<td>$B$</td>
<td>$aapt^C(2)$</td>
<td>$1$</td>
<td>$D$</td>
<td>$capt^2_D$</td>
<td>$C$</td>
<td>$aapt^D(2)$</td>
<td>$1$</td>
</tr>
<tr>
<td>$C$</td>
<td>$capt^4_C$</td>
<td>$B$</td>
<td>$aapt^C(4)$</td>
<td>$1$</td>
<td>$D$</td>
<td>$capt^4_D$</td>
<td>$C$</td>
<td>$aapt^D(4)$</td>
<td>$1$</td>
</tr>
<tr>
<td>$C$</td>
<td>$capt^6_C$</td>
<td>$B$</td>
<td>$aapt^C(6)$</td>
<td>$1$</td>
<td>$D$</td>
<td>$capt^6_D$</td>
<td>$C$</td>
<td>$aapt^D(6)$</td>
<td>$1$</td>
</tr>
<tr>
<td>$C$</td>
<td>$capt^8_C$</td>
<td>$B$</td>
<td>$aapt^C(8)$</td>
<td>$1$</td>
<td>$D$</td>
<td>$capt^8_D$</td>
<td>$C$</td>
<td>$aapt^D(8)$</td>
<td>$1$</td>
</tr>
<tr>
<td>$C$</td>
<td>$capt^1_C$</td>
<td>$E$</td>
<td>$aapt^C(1)$</td>
<td>$1$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$C$</td>
<td>$capt^3_C$</td>
<td>$E$</td>
<td>$aapt^C(3)$</td>
<td>$1$</td>
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<td></td>
</tr>
<tr>
<td>$C$</td>
<td>$capt^5_C$</td>
<td>$E$</td>
<td>$aapt^C(5)$</td>
<td>$1$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$C$</td>
<td>$capt^7_C$</td>
<td>$E$</td>
<td>$aapt^C(7)$</td>
<td>$1$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$B$</td>
<td>$aapt^B(1)_B$</td>
<td>$E$</td>
<td>$aapt^B(1)$</td>
<td>$2$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$B$</td>
<td>$aapt^B(5)_B$</td>
<td>$E$</td>
<td>$aapt^B(5)$</td>
<td>$2$</td>
<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$E$</td>
<td>$aapt^E(4)_E$</td>
<td>$B$</td>
<td>$aapt^E(4)$</td>
<td>$2$</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$E$</td>
<td>$aapt^E(8)_E$</td>
<td>$B$</td>
<td>$aapt^E(8)$</td>
<td>$2$</td>
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<td></td>
</tr>
<tr>
<td>$B$</td>
<td>$aapt^B(3)_B$</td>
<td>$A$</td>
<td>$aapt^B(3)$</td>
<td>$2$</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$B$</td>
<td>$aapt^B(7)_B$</td>
<td>$A$</td>
<td>$aapt^B(7)$</td>
<td>$2$</td>
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<td></td>
</tr>
<tr>
<td>$B$</td>
<td>$aapt^E(1)_B$</td>
<td>$D$</td>
<td>$aapt^E(1)$</td>
<td>$3$</td>
<td></td>
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<td></td>
</tr>
<tr>
<td>$E$</td>
<td>$aapt^E(2)_E$</td>
<td>$D$</td>
<td>$aapt^E(2)$</td>
<td>$2$</td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>$E$</td>
<td>$aapt^E(6)_E$</td>
<td>$D$</td>
<td>$aapt^E(6)$</td>
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<td></td>
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<tr>
<td>$E$</td>
<td>$aapt^B(4)_E$</td>
<td>$D$</td>
<td>$aapt^B(4)$</td>
<td>$3$</td>
<td></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>$A$</td>
<td>$aapt^A(1)_A$</td>
<td>$D$</td>
<td>$aapt^A(1)$</td>
<td>$2$</td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>$A$</td>
<td>$aapt^A(5)_A$</td>
<td>$D$</td>
<td>$aapt^A(5)$</td>
<td>$2$</td>
<td></td>
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<td></td>
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</tr>
</tbody>
</table>

8. David encounters Elizabeth

At time $t_8$, David encounters Elizabeth. David picks his $DL_1$, and Elizabeth picks her $DL_2$. They give distributing-ACs in their picked $DL$s to each other and update their reply tables, as shown in Table 4.26 and Table 4.27.

After David gives Elizabeth the distributing-ACs, Elizabeth gets a ready-AC $AC^{1[3]}_{A,D}$.  

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Then Elizabeth has 1 ready-AC, while David has 2 ready-ACs, so that David has only one more ready-ACs than Elizabeth. That is the reason why David does not give his own ready-ACs to Elizabeth, even though Elizabeth trusts David.

We assume that Elizabeth does not get $AC^{1[3]}_{A,D}$, so that she has no ready-AC. Then David should give her a ready-AC from his own two randomly.

Table 4.26: David and Elizabeth’s AC Lists at Time $t_8$

<table>
<thead>
<tr>
<th></th>
<th>DL1</th>
<th>Before $AC^{1[0]}_D, AC^{3[0]}_D, AC^{5[0]}<em>D, AC^{7[0]}<em>D, AC^{2[2]}</em>{E,C}, AC^{1[2]}</em>{A,C}$</th>
<th>After $AC^{2[2]}<em>{E,C}, AC^{3[2]}</em>{C,E}, AC^{4[2]}_{A,E}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RL</td>
<td>Before $AC^{1[3]}<em>{E,C}, AC^{4[3]}</em>{B,C}$</td>
<td>After $AC^{1[3]}<em>{E,C}, AC^{4[3]}</em>{B,C}$</td>
</tr>
<tr>
<td></td>
<td>RL</td>
<td>Before $\emptyset$</td>
<td>After $AC^{1[3]}_{A,D}$</td>
</tr>
</tbody>
</table>
Table 4.27: David and Elizabeth’s Relay Table At Time $t_8$

<table>
<thead>
<tr>
<th>David</th>
<th>Elizabeth</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_d^{old}$</td>
<td>$A_{apt}^{old}$</td>
</tr>
<tr>
<td>$D$</td>
<td>$capt_D^7$</td>
</tr>
<tr>
<td>$D$</td>
<td>$capt_D^4$</td>
</tr>
<tr>
<td>$D$</td>
<td>$capt_D^6$</td>
</tr>
<tr>
<td>$D$</td>
<td>$capt_D^8$</td>
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<tr>
<td>$D$</td>
<td>$capt_D^1$</td>
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<tr>
<td>$D$</td>
<td>$capt_D^3$</td>
</tr>
<tr>
<td>$D$</td>
<td>$capt_D^5$</td>
</tr>
<tr>
<td>$D$</td>
<td>$capt_D^7$</td>
</tr>
<tr>
<td>$C$</td>
<td>$aapt_C^{(1)}$</td>
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</tbody>
</table>

4.8.2 Queries and Replies

We still use the previous example and assume that the delivery of queries and replies cost little time so that no AC expires in the period.

We assume that David wants to send a query to the LBS. He chooses a AC (e.g. $AC_{E,C}^{[3]}$) from his two ACs (i.e., $AC_{E,C}^{[3]}$ and $AC_{B,C}^{[3]}$) randomly. If we review the previous tables, we learn that $AC_{E,C}^{[3]}$ is generated by Elizabeth and has 3 agents (i.e., Elizabeth,
Bob and Charlie). When David uses the AC to send his query, the sender identity of the query is Elizabeth. The Capt (i.e., $capt^1_E$) is also included in the query. Then David uses the identity of the last agent (i.e., Charlie) and the Aapt (i.e., $aapt^{E(1)}_C$) to generate a pseudonym $psd^{E(1)}_c = \mathrm{pseudo}\left(Charlie,aapt^{E(1)}_C\right)$, which is used as a temporary identity of David before he receives the reply. Besides, $AC^{[3]}_{E,C}$ cannot be given to any user until it expires. The process is shown in Figure 4.10.

![Figure 4.10: David’s Query](image)

The LBS sends a reply message to Elizabeth based on the sender identity of the query. The Capt (i.e., $capt^1_E$) is also included in the reply. If an attacker learns these messages, he believes that it is Elizabeth who sends the query.

When Elizabeth receives the reply message, she searches her reply table for the AC used in the reply message, as shown in Table 4.27. Since the message is sent by the LBS, the $Aid_{old}$ should equal to her own identity, and the $Aapt_{old}$ should equal to the Capt. Then she must find an entry like Table 4.28, which enables Elizabeth to modify the reply message and forward it to Bob, as shown in Figure 4.11.

![Table 4.28: Elizabeth’s Reply Table Entry](image)
If Bob receives the reply message successfully, he checks his reply table as shown in Table 4.21. He finds an entry whose $A_{old} = \text{Elizabeth}$ and $A_{apt,old} = aapt_{E}^{(1)}$, as shown in Table 4.29. In the same way as Elizabeth, Bob forwards the reply message to Charlie, as shown in Figure 4.12.

When the Charlie receives the reply message from Bob, Charlie learns that he is the last agent based on his reply table as shown in Table 4.25 and Table 4.30, because the $EQL$ is equal to 3. He ignores the record of $ID_{nxt}$ $D$ and views it as a $VOID$ because he is the last agent.
To forward the reply message to the unknown original requester (i.e., David), Charlie generates a pseudonym $\text{psd}_c^{E(1)} = \text{pseudo}\left(Charlie, aapt_c^{E(1)}\right)$ using his own identity and $Aapt_{\text{new}}$. We should notice that the pseudonym is exactly the temporary identity of David. David then modifies the reply message and forwards it, as shown in Figure 4.13.

$$\text{pseudo}\left(Charlie, aapt_c^{E(1)}\right) \Rightarrow \text{psd}_c^{E(1)}$$

When a user who carries $\text{Reply}_c^{E(1)}$ encounters David, the user forwards the reply to him, so that David gets his reply.

### 4.9 Experiment

We used the map of Helsinki in our simulator to evaluate performance of the proposed ACP. We compare ACP with Binary Spray and Wait (BSW) protocol [25], distributed social-based location privacy protocol (SLPD) [30] and our Multi-Hop Location-Privacy Protection (MHLPP). We simulated the continuous movement of users along streets on the map with one LBSP, fixed at a random location on the map.
For each user, we associate a random social value between 0 - 100%, each corresponding to other users. Since each social value is assigned with equal probability, we can compute the expected number of friends of an user. If an user whose social value is larger than 85% is called a friend and there are $n$ users in the network, then there are $n \times (1 - 85\%)$ friends for this user in consideration.

The Shortest Path Map-Based Movement (SPMBM) [11] is used in our experiment for the user mobility model. For each experiment, we give the simulator a random seed so that it can generate a pseudo-random number based on the seed. Therefore, all the factors including users’ speed and locations are the same if two experiments have the same random seed. All four protocols are tested using the same set of random seeds.

Before each experiment, the simulator runs for 800 seconds, and then we pick 100 users out of 126 users randomly to send a query to the LBSP. The simulation then lasts for 20 minutes before we measure different parameters for performance analysis.

### 4.9.1 Average Query Success Ratio

The query success ratio is the percentage of delivered queries among some attempts. Since users sending 100 queries in each experiment, if $s$ queries are delivered to the LBSP at time $t$, the query success ratio of time $t$ is $s\%$.

As shown in Figure 4.14, we compare the average query success ratio of the four protocols for 5 different communication ranges (10, 30, 50, 70 and 90 meters) at 10 minutes mark. We observe that our ACP and BSW achieve high query success ratio, while the query success ratio in case of MHLPP and SLPD are lower than the other two. BSW has the highest query success ratio because it is a no-privacy protocol. The ACP has slightly lower query success ratio than BSW, because the query delivery process of the ACP is almost the same as that of BSW. Since users of ACP must wait for available ACs, it requires more time to initiate their queries. However, ACP and BSW exhibit similar performance
compared to the other two protocols. MHLPP and SLPD need to find friends to obfuscate their queries, which complicates their query delivery process.

The results at 20 minutes mark is shown in Figure 4.15. Both MHLPP and SLPD give much higher query success ratio after 20 minutes than after 10 minutes. That is because they require more time in their obfuscation phases when they need to find friends. In fact, some of the queries of MHLPP and SLPD still do not finish their obfuscation phase at 20 minutes mark.
The communication range can influence the query success ratio. In most of the cases, the success ratio rises when we increase the communication range, and its influence is especially evident under 50 meters. A large communication range makes it easy for users to encounter others, which is good for them to forward queries. However, an user who is so far away from the destination does not want the intermediates of his query encounters many users nearby. Because all users who carry copies of that query are near the sender instead of the destination, which decreases their query success ratio. Therefore, when the communication range reaches 70 meters, the success ratios almost stay flat.

In Figure 4.16, we observe that both ACP and BSW have better convergence speed than MHLPP and SLPD. In other words, the former two protocols approach the 100% query success ratio mark faster than the latter two. At the very beginning, the ACP even has a little higher query success ratio than BSW. Because the ACP users need ready AC, and most of the users get their first ready-ACs at places where there are many users, users rarely generate query near the edges of the map at the beginning, which facilitates their queries delivery process. For example, if an user generates his query at the edge of the map.
map, the copies of this query might be sent to users who are also at the edge, and it takes more time for them to deliver the query. If the user does not generate his query until he arrives at a place near the center, the copies of this query will be carried by the users in the center with higher probability.

Figure 4.16: Average Query Success Ratio for 50-Meters Communication Range

4.9.2 Average Reply Success Ratio

When the LBSP receives a query, it sends a reply to the requester. If the reply reaches the original requester before the test ends, we view it as a success; otherwise, the reply is considered to be failed. There are three reasons for not receiving reply: 1) the query is not delivered to the LBSP successfully; 2) the query took too much time for which the reply could not be delivered in time; or 3) the route of the reply is too long. Since there are 100 queries in each experiment, we expect the number of replies should be 100.

In Figure 4.17, the BSW has a significantly higher reply success ratio than all other protocols, because it is a no-privacy protocol. ACP has a higher ratio than MHLPP and
SLPD, but its advantage is not as large as that in the query process. In fact, the reply process of MHLPP and SLPD are simpler than that of the ACP, but the ACP saves much time in its query process so that it has a better reply success ratio than the other two.

![Average Reply Success Ratio for 50-Meters Communication Range](image)

**Figure 4.17: Average Reply Success Ratio for 50-Meters Communication Range**

### 4.9.3 Total Number of Query Relays

The query delivery process of all the four protocols use store and forward strategy, and BSW makes copies for queries and gives half of the copies to any users it encounters. That is a significant cost for the network, so we use the number of query relays (QR) to evaluate that cost. The QR is initialized as zero at the beginning of the test. When an user relays one or several copies of a query, we increase QR by 1. For example, in SLPD, there are two phases: the obfuscation phase and the free phase. In the obfuscation phase, a query is forwarded among one-hop friends for $k$ times. After that, it is forwarded using BSW protocol. BSW makes $c$ copies of the query and gives half of the copies to any encountering user. Thus, QR should be roughly $k+c$. Since the user gives all its copies to the destination
at once if he encounters the destination, the QR may be smaller. The smaller that number
is, the smaller the cost of the network is. Since there are 100 queries, we divide QR by 100
to get an average value.

In Figure 4.18, we compare QR in all four protocols. We observe that both BSW
and ACP have slightly lower QR than the other two. In case of ACP and BSW, they
deliver queries so fast that users who carry more than one copy give all their copies to the
destination before they send these copies to different users separately. As a result, many
copies have no chance to be forwarded, which decreases the cost.

While both MHLPP and SLPD have obfuscation phases, the queries start to be deliv-
ered freely (as in BSW) at a random place which might be so far away from the destination,
so that almost all copies can be forwarded.

![Figure 4.18: Average Number of Forwarding Queries At 20 Minutes Mark](image)

The communication range affects the total number of forwarding queries, especially in
the case of MHLPP and SLPD. These two protocols can finish their obfuscation phase more
quickly in a larger communication range scenario, so that more queries can be forwarded
freely (as in BSW), which makes their QR larger.
4.9.4 Memory Cost

We count the number of queries carried by each user to evaluate the memory cost of the four protocols. Several copies of the same query are counted as one.

In Figure 4.19, we compare the number of queries per user in all four protocols at 20 minutes mark for different communication ranges. We observe that BSW has the highest value in most of the cases whereas ACP always stays at a similar level as BSW. The average query buffer needed per user in the other two protocols (MHLPP and SLPD) increases with the increase in the communication range. The MHLPP even exceeds BSW when the communication range is 90 meters. The reason is that quite a number of users in BSW and ACP forward their copies to the destination so that there is no copy left with them at 20 minutes mark, while the rest of them cannot forward their copies to the destination even with large communication ranges. At the same time, the number of the other two protocol’s free phase queries is significantly influenced by the communication range. The more queries we have in the free phase, the more copies there are in the network.

![Figure 4.19: Average Number of Query Buffer Needed at 20 Minutes Mark](image_url)
The Figure 4.20 shows the average number of queries which are carried by users in communication ranges 10, 50 and 90 meters. The curves for ACP and BSW rise sharply at the beginning and then become flat, while those for MHLPP and SLPD rise smoothly and continuously.

4.9.5 Distributing Appointment Cards

Exchanging ACs is a feature of proposed ACP, which can be considered as an extra cost. We count the number of exchanging ACs per minute to evaluate this extra cost of ACP.

In Figure 4.21, we show the total number of exchanging ACs in the whole network. For example, if an user Alice encounters another user Bob, the total number of exchanging ACs processes increases by one when Alice exchanges any ACs to Bob. We count the number of those exchanging processes occur per minute. As shown in the figure 4.21, the exchanging processes do not occur frequently, but about 2 times per minutes. Since the size of an AC is small, it does not consume too much network resource. At the same time, users can get many ACs to help them send queries, as shown in Figure 4.22. The number of ready ACs per user is raising smoothly and steadily.
(a) communication range is equal to 10 meters

(b) communication range is equal to 50 meters

(c) communication range is equal to 90 meters

Figure 4.20: Average Number of Queries Carried Per User
Figure 4.21: Average Number of Exchanging ACs Per Minute Under Different Communication Ranges

Figure 4.22: Average Number of Ready ACs Per User
Chapter 5

OMSN Routing Simulator (ORS)

The Opportunistic Networking Environment (ONE) [11] is a simulator designed for evaluating DTN routing and application protocols. Researchers can import real-world map into the simulator so that hosts walk along streets and roads in the simulator. The movement model of hosts can be defined by researchers, which enables researchers to evaluate the performance of their protocols in different scenarios. The User Interface of the ONE is also friendly, where researchers can observe the movement of all hosts. When a round of experiment ends, ONE outputs the results to a defined file. The simulator can also execute in console mode, which allows a higher experiment speed.

The ONE is an excellent simulator for DTN research, while it has its own weakness. The way that ONE estimates the distance between two hosts is not thorough, which may lead to inaccurate results. When a host broadcasts a message, only the hosts which are in its communication radius should receive the message. If the simulator cannot give the accurate set of hosts which can receive the message, the experiment result is not reliable. Although we can avoid this problem by setting parameters carefully, this problem cannot be completely ignored. Besides, some movement models need to calculate shortest path several times, which may require several seconds. Even though that is not a long time, it can slow down the experiment speed significantly as the total time of a round of experiment
In this chapter, we introduce two major algorithms used in our new ORS simulator. The vertex reduce algorithm is used for simplifying the input of the all-pair shortest path algorithm, so that the simulator can initialize quickly. The finding nodes algorithm is used to find users which are in the communication radius of a given user.

5.1 Overview

At its core, ORS is a discrete event simulation engine. To simulate an OMSN, hosts can move in the simulator, and information of social network is also included in the simulator. The simulator reads real-world maps, which enables hosts to walk along streets on the maps. The default movement model of hosts is Working day movement model [5] where hosts walk through the shortest path between several random points. Researchers can replace the movement model with other models by implementing models in the source codes.

The main function of ORS can be considered as the movement of hosts and message routing. The movement routes of hosts is generated based on the movement model and are defined by a series of segment lines before the simulation starts. In other words, the routes are fixed before hosts start to walk so that the locations of hosts is a function of time. Since ORS can get the locations of hosts directly when given a specific time value, it only calculate locations of hosts when some hosts send messages or UI needs the locations of hosts. Each host has a communication range which is a circle. ORS calculates the locations of hosts when one or more hosts send messages, and the hosts inside the communication range must receive the sent messages. The messages are always broadcast, and ORS copies them to all hosts inside the communication range of the host who sends the message. Therefore, the host itself decides whether a received message should be received or not, which enables the hosts to control as many details as possible. The message structures
are defined by the implementation of DTN routing protocols and do not have mandatory entries except a unique ID assigned by the simulator which is used for identifying messages.

The UI of ORS is shown in Figure 5.1. The parameters of the simulator which include the file path of the map file, the number of hosts, the communication range and so on are defined in a “txt” file. When we use ORS open the “txt” file (e.g., “aenv1.txt”), ORS reads all parameters in the file and initialize the simulator. First, the simulator draws the map and uses yellow lines to denotes the streets; second, ORS generates hosts, their relationship strength, and their movement routes; third, ORS initializes instances of a specific routing protocol for each host. ORS starts the experiment automatically when the initializations finish. Users can define the values of the textboxes on the UI in source codes so that they can debug their protocols.

![Figure 5.1: Simulator UI](image)

The hosts in the simulator can be viewed as mobile devices (e.g., smartphones) which are a leak of software. These devices are carried by people who are moving in the sim-
ORS offers the devices interfaces so that users can implement routing protocols which is the software of the mobile devices. The interfaces which devices can get from ORS includes setting timers, current time, the identities of their owners, sending messages to surroundings and so on. Comparing to ONE, the interfaces of ORS are more flexible so that developers can almost define everything when they implement their routing protocols, like the size of buffers or the frequency of sending hello messages. ORS leaves the implementation of persistent storage, energy consumption and message routing to routing protocols instead of giving interfaces of these features, which enables researchers to make their experiments more accurate. For example, the sizes of the messages are different. the hello messages are small while general messages are large. Also, different operations cost different energy. Therefore, it is good for developers to define these features by them self. ORS can track all messages if developers implement the method by which ORS can identify messages. In this way, researchers can learn the location of each message, the number of the message which is delivered to the destination, and the state of each message (e.g., shipping or delivered).

The relationship strengths of each pair of hosts are defined when ORS initials hosts. The relationship strengths are fixed during the experiment. All relationship strengths are recorded in a table so that routing protocols can get the relationship between any pair of hosts when the protocols learn their identities. In general case, the routing protocols can learn the identity of their owners and the identity of the senders of messages, so that routing protocols can get the relationship strengths between the senders and their owners.

5.2 Vertex Reduction Algorithm

Movement of network nodes is a significant factor in the performance of DTNs. To evaluate the performance of different DTN protocols, researchers have presented different kinds of movement models, like in [5]. Since shortest path algorithm is an essential and time-cost
part of creating many movement models, it is an important aspect to optimize the time-cost for simulators, calculating the all-pairs shortest paths in the entire map.

The best known non-negative edge weight undirected map all-pairs shortest path algorithm [21] has a complexity $O(n^2 \log n)$, which is still expensive when $n$ is huge. For most real-world city maps, there are thousands of points in a single square kilometer. Since a ten-square kilometers map is reasonable for a DTN protocol evaluation, a simulator must cut down the time spent in calculating all-pairs shortest paths to speed up the experiment.

Real-world map developers often use short straight lines to present curves, like in [1], so that a several-meters curves may contain tens of points. It is obvious that we do not need to calculate shortest path for every one of these points. In this chapter, we present an Vertex Reduction Algorithm (VRA) to reduce the number of points before the use of the shortest path algorithm. The basic idea is that VRA removes all points whose degrees are less than 3 from the map, while keeping the result of all-pairs shortest path algorithm correct.

The rest of this chapter is organized as follows. Section 5.2.1 presents some basic definitions and lemmas. The process of VRA is described in Section 5.2.2 and Section 5.2.3.

### 5.2.1 Ignorable Vertex and Reserved Vertex

Vertices in the graph are considered ignorable and/or reserved (definition follows). In each iteration of VRA, we remove the ignorable vertex from the graph, while the reserved vertices compose a new graph.

**Definition 1**: The vertex whose degree is larger than 2 is the reserved vertex (denoted by $R$).

**Definition 2**: The vertex whose degree is smaller than or equal to 2 is called the ignorable vertex (denoted by $G$).
**Definition 3**: If two reserved vertices (e.g. $R_1, R_2$) are connected by a sequence of ignorable vertices (e.g. $G_1, G_2, \cdots, G_n$), then the sequence from $R_1$ to $R_2$ (i.e., $R_1, G_1, G_2, \cdots, G_n, R_2$) is a line-segment (denoted by $LS$).

A reserved vertex can belong to different line-segments, while an ignorable vertex belongs to a unique line-segment. Both the reserved vertex and the ignorable vertex are called vertices ($V$).

**Definition 4**: The shortest route between two vertices inside a segment-line is called the inner shortest path ($SPI$).

Let $SPI(V_i, V_j)$ denote the inner shortest path between two vertices (i.e., $V_i, V_j$) inside a segment-line.

**Lemma 1**: If two vertices (i.e., $V_i, V_j$; $i < j$) are in the same line-segment, the shortest path between them is

$$SP(V_i, V_j) = \min \{SPI(V_i, V_j), SPI(R_1, V_j) + SPI(V_j, R_2) + SP(R_1, R_2)\} \quad (5.1)$$

**Proof**: Lemma 1 is shown in Figure 5.2. We assume that there is a path (e.g., $V_i - V_x - V_j$) whose length is smaller than or equal to Equation 5.1 between $V_i, V_j$, where $V_x$ is a vertex in the segment-line including $V_i, V_j$.

![Figure 5.2: Shortest Path On A Single Segment-Line](image)

Case 1: $V_x$ is between $V_i$ and $V_j$. The length of the path $V_i - V_x - V_j$ must be equal to...
SPI \((V_i, V_j)\) or there must be duplicated vertices on the path.

Case 2: \(V_x\) is between \(R_1\) and \(V_i\) or between \(V_j\) and \(R_2\). \(V_i - V_j\) should not be a part of the path or \(V_i - V_j\) could be the shortest path. Then the path \(V_i - R_1 - R_2 - V_j\) must be a part of \(V_i - V_x - V_j\) because \(R_1\) and \(R_2\) are entrances of the segment-line.

Since an all-pairs SPI has a complexity of \(O(n^2)\) and the \(n\) here is much smaller than the number of points on the entire map, the time-cost for SPI is ignorable comparing to the time-cost of the entire map all-pairs shortest path calculation.

**Lemma 2:** We assume that there are two different line-segments

\[LS_i = \{R_{i1}, G_{i1}, G_{i2}, \ldots, G_{in}, R_{i2}\}\] and \(LS_j = \{R_{j1}, G_{j1}, G_{j2}, \ldots, G_{jm}, R_{j2}\}\). We pick a vertex \(V_i\) from \(LS_i\) and a vertex \(V_j\) from \(LS_j\), then the shortest path between \(V_i\) and \(V_j\) is

\[
SP(V_i, V_j) = \min\{SP(V_i, R_{i1}, R_{j1}, V_j), SP(V_i, R_{i2}, R_{j1}, V_j), SP(V_i, R_{i1}, R_{j2}, V_j), SP(V_i, R_{i2}, R_{j2}, V_j)\} \quad (5.2)
\]

where \(SP(V_i, R_{ia}, R_{jb}, V_j) = SP(V_i, R_{ia}) + SP(R_{ia}, R_{jb}) + SP(R_{jb}, V_j)\). Here \(V_i\) and \(R_{ia}\) are in the same line-segment, so we can use Lemma 1 to calculate \(SP(V_i, R_{ia})\), so does \(SP(R_{jb}, V_j)\). The \(SP(R_{ia}, R_{jb})\) is the only part we need to calculate using all-pair shortest path algorithms. We should notice that \(R_{ia}\) and \(R_{jb}\) could be the same vertex, but it does not make any difference to the lemma.

**Proof:** Since \(V_i\) and \(V_j\) are not in the same segment-line, there must be one or more reserved vertices on their shortest path. On \(V_i\)'s side, one of \(R_{i1}\) and \(R_{i2}\) must be on the shortest path. One of \(R_{j1}\) and \(R_{j2}\) should be on that shortest path, either. We assume that \(R_{iu}\) and \(R_{ju}\) are on the shortest path between \(V_i\) and \(V_j\), then a shortest path between \(R_{iu}\) and \(R_{ju}\) should be a part of that path.
5.2.2 Vertex Reduction

VRA iteratively removes ignorable vertices from the graph until only reserved vertices remain. In each iteration, we remove all ignorable vertices from the graph but keep the edges. If there are different routes between a pair of reserved vertices, we keep the shortest one and remove others.

5.2.2.1 Remove Ignorable Vertices

Since the degree of ignorable vertices is no more than 2, an ignorable vertex has only 0, 1 or 2 neighbours. In the case of 0 or 1 neighbour, we simply delete the ignorable vertex; if it has two neighbours, we connect its two neighbours before it is removed, as shown in Figure 5.3. When we remove an ignorable vertex, the weight of the line which connects its two neighbours is equal to the sum of its recent two lines’ weights (i.e., $W_l + W_r$). After we remove all ignorable vertices in a line-segment, the two reserved vertices at the end of the line-segment are connected with a line directly, whose weight is the sum of all the intermediate ones’ (i.e., $W_1 + W_2 + W_3 + W_4$).

![Figure 5.3: Remove Ignorable Vertices](image)

5.2.2.2 Remove Redundant Connections

After we remove all ignorable vertices, all the reserved vertices are connected directly. However, it is possible that there are several connections between a pair of reserved vertices. Since the shortest route between a pair of neighbouring vertices makes other longer ones
redundant, we remove all routes except the shortest one, as shown in Figure 5.4. We assume that $W_2$ is the shortest line among three connections, when $W_1$ and $W_3$ are removed.

![Figure 5.4: Tidy Reserved Connections](Image)

### 5.2.2.3 Iterations

The process is shown in Algorithm 5.1. The input of the algorithm is the original entire map, which is called $Graph_0$. In the $i^{th}$ iteration, VRA makes a copy of $Graph_i$ as $Graph_{i+1}$. If $i > 0$, the $Graph_i$ is the output of the previous (i.e., $(i - 1)^{th}$) iteration. VRA removes all ignorable vertices in the $Graph_{i+1}$ as described in Section 5.2.2.1 and remove all unnecessary routes between reserved vertices as described in Section 5.2.2.2. In other words, $Graph_i$ gets smaller and smaller as $i$ increases, because we always remove ignorable vertices from them. If $Graph_i$ is equal to $Graph_{i+1}$, which means that the $i^{th}$ iteration makes no modification on the graph, the algorithm ends.

### 5.2.3 Assembling Vertices

We assume that the vertex reduction process stops at the $i^{th}$ iteration. Then, the $Graph_i$ is the input of an all-pairs shortest path algorithm. Let $SP_i(R_u, R_v)$ denote the shortest path from $R_u$ to $R_v$ in $Graph_i$. We can infer the all-pairs shortest path of $Graph_{i-1}$ based on $Graph_i$ with Lemma 1 and Lemma 2. The algorithm ends when we get the result of $Graph_0$. The algorithm is shown in Algorithm 5.2.

We start from the $Graph_{i-1}$ and assemble all intermediate graphs, until we get the result of $Graph_0$. For any intermediate $Graph_j$, we already have the all-pairs shortest path
Algorithm 5.1 Algorithm For Vertex Reduction

1: procedure REDUCE(Graph_i)
2:   Copy Graph_i to Graph_{i+1}
3:   for every ignorable vertex G_u in Graph_{i+1} do
4:     remove(G_u)
5:   end for
6:   for every pair of reserved vertices do
7:     remove redundant connections
8:   end for
9: end procedure

10: procedure VRA(Graph_0)
11:   i = 0
12:   while i = 0 or there is any difference between Graph_{i-1} and Graph_i do
13:     REDUCE(Graph_i)
14:     i = i + 1
15: end while
16: end procedure

Algorithm 5.2 Algorithm for Assembling Ignorable Vertices

1: procedure ASSEMBLE(Graph_i)
2:   for all ignorable vertices (G_u) in Graph_i do
3:     for all other vertices (G_v) in Graph_i do
4:       if G_u and G_v are in the same line-segment then
5:         Use Lemma 1 to calculate their shortest path.
6:       else
7:         Use Lemma 2 to calculate their shortest path.
8:     end if
9:   end for
10: end procedure

11: procedure ASSEMBLE_ALL(i)
12:   while i > 0 do
13:     ASSEMBLE(Graph_{i-1})
14:     i = i - 1
15: end while
16: end procedure
result of its reserved vertices in the previous iteration (i.e., $Graph_{j+1}$). Then, we calculate the shortest path from any ignorable vertex to all others. When the two vertices are in the same line-segment, we use Lemma 1 to calculate their shortest path. The Lemma 1 includes four parts: $SPI(V_i, V_j), SPI(R_1, V_i), SPI(V_j, R_2)$ and $SP(R_1, R_2)$. Since we already have the result of $SP(R_1, R_2)$ in the previous iteration, we just need to calculate the remaining three $SPI$ parts, which is easy and has fewer nodes. If the two vertices are in different line-segments, we use Lemma 2 to calculate the shortest path. We already have all the $SP$ parts from the previous iteration, so we just need to deal with their respective $SPI$ parts.

### 5.3 Finding Nodes in a Range

We assume that there are $n$ nodes in a planar map (size: $h \times w$). Those nodes keep moving on the map slower than a speed threshold ($S$). If the distance between two nodes $a$ and $b$ is smaller than $r$, they are considered connected. We want to calculate all-pairs connections for all nodes on the map periodically.

If we calculate these connections directly, the complexity is $O\left(\frac{n^2}{2}\right)$. We assume that $r \ll \min\{h, w\}$, and nodes are distributed on the entire map symmetrically. Then, the expected number of nodes which has a connection with a node $(v)$ is $\frac{n}{h \times w} \times \pi r^2 \ll n$. If we traverse all other $(n - 1)$ nodes of $v$, it will be a waste of time.

We propose an algorithm to optimize the calculation of all-pairs connections. We draw grids whose size is $l \times l$ on the map. When we calculate connections of the node $v$, only nodes in surrounding grids will be traversed.
5.3.1 Static Nodes

If nodes on the map are stationary, the $r$ is the only factor of the selection of the grid size $(l \times l)$. The length $l$ of the side of a grid should be equal to $r$, as shown in Figure 5.5. For any node $v$ in the dark grid, all nodes whose distance between them is equal to or shorter than $r$ should be in the grey or dark grid. Therefore, if we want to get all connected nodes to node $v$, we simply need to traverse all nodes in the grey and dark grids instead of all nodes in the entire map. In this case, the expected number of nodes which we need to traverse is $\frac{9n \times r^2}{h \times w}$ for checking connections for a node $v$. If we calculate connections for all nodes, we simply need to get the distances of about $\frac{9n^2 \times r^2}{2 \times h \times w}$ pairs of nodes, instead of $\frac{n^2}{2}$ pairs.

![Figure 5.5: Grid Size For Still Nodes](image)

5.3.2 Mobile Nodes

The problem is a bit more complicated if nodes are moving. Assuming that we want to calculate all-pairs connections at $t_1$, first, we draw grids at time $t_0$, so that we know which grid is a node in at $t_0$. Instead of $t_0$, we want to get connections at $t_1$. In this case, the length $l$ should be larger than $r$.

Suppose that we have two nodes $u$ and $v$, and their distance is $d_1$ at $t_1$. Since the
maximum speed of nodes is $S$, their distance $d_0$ at $t_0$ satisfies

$$\max \{0, d_1 - 2\delta\} \leq d_0 \leq d_1 + 2\delta$$

where $\delta = S|t_1 - t_0|$. When $d_1 \leq r$, these two nodes are connected at $t_1$, then $d_0$ must satisfy $0 \leq d_0 \leq r + 2\delta$. As shown in Figure 5.6, If we draw grids on the map in an attempt to place the two nodes in the same or adjacent grids at $t_0$, the length of each grid $l = r + 2\delta$.

![Figure 5.6: Length of Grid](image)

5.3.3 Complexity

The complexity of drawing grids is $O(n)$, while that of checking connections is $O\left(\frac{9n^2 \times r^2}{2 \times h \times w}\right)$, so the checking part is much more expensive than the drawing part. Since $l = r + 2\delta = r + 2S|t_1 - t_0|$, the checking part achieves its best performance when $t_1 - t_0 = 0$, then its complexity is $O\left(\frac{9n^2 \times r^2}{2 \times h \times w}\right)$. That is equal to the complexity when nodes are stationary.
Chapter 6

Conclusion and Future Work

In this chapter, we will summarize our findings and discuss the future directions of the proposed work in the previous chapters yet to be explored.

6.1 Summary of Work Done

In this thesis, we proposed and analyzed two new location-privacy preserving protocols, namely MSLPP and ACP, besides developing a new OMSN simulator, called ORS, as a platform for evaluating the proposed protocols and comparing them with their counterparts.

Our first protocol, MSLPP, is a distributed location-privacy preserving protocol using social-relationship and encryption. Simulation results show that it has a better performance on delivery success ratio and provides an acceptable obfuscation compared to its counterpart HSLPO which is an improvement of their earlier scheme SLPD. Compared to HSLPO, our scheme MHLPP achieves an increase in success ratio between 6% and 11% for the same range of parameters considered by the authors of SLPD. The success ratios of both HSLPO and MHLPP decline when the privacy threshold is increased, while the success ratio of HSLPO is always lower than that of MHLPP and decreases more sharply.
than that of MHLPP. Although HSLPO is slightly more secure than MHLPP based on our experiments which means the original requester has a lower rate to be located, but the entropy difference is quite small and negligible. Encryption and decryption to enhance security are added cost for MHLPP which is acceptable. Our experiment (using the map of Helsinki) presents that in a social network with 126 users, the average number of times of a query is encrypted and decrypted is less than 3 when the privacy threshold is considered as 85.

Our second proposed Appointment Card Protocol ACP also uses social relationship for preserving location privacy. It facilitates the obfuscation process by continuously exchanging appointment cards among users so that the original requester does not communicate with any of its friends when initiating a query. Simulation results show that it has a better performance with respect to the query-delivery success ratio and provides an acceptable obfuscation compared to its counterparts. Although ACP requires slightly more time to forward the reply, the total time required for query delivery and reply delivery is still less than that for its counterparts SLPD and MHLPP.

To facilitate our experimentation, we have developed a simulator, called ORS, which is more suitable for OMSN simulation than the existing simulator, ONE. The ORS is more reliable and efficient than ONE for simulating opportunistic social networks.

6.2 Future Work

In MHLPP, we just considered the relationship strength between two connected people in the social network; in other words, an agent only gives the message to his direct friend. In most of the cases, the friends of your friends can also be trusted and be considered. If these friends can participate in forwarding queries, agents can have more choice in the obfuscation phase.

In ACP, the sizes of agents’ relay tables are significantly affected by the number of
appointment cards passing by them. If we can decrease the number of appointment cards in the network, the burden of agents can also decline. For example, a single appointment card can be shared among friends instead of being used by only one user.
References


